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Feed strategies in dairy production

- Economic implications of using by-products in the feed ration

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- Economic implications of using by-products in the feed ration

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Erik Johansson and Kristoffer Persson

Summary

An increased competition on the world market of dairy products and a price setting process highly influenced by the world market price have led to drop in profitability for the Swedish dairy farmers. This creates interest for cost saving opportunities in the dairy production among dairy farm managers. The single most expensive cost in dairy production is the feed cost. Hence, the subject of this thesis is the profitability of feed strategies in dairy production.

The study focuses on the determining factors of the competitiveness associated with farm feeding operations. This study employs income over feed cost, IOFC, as a valid evaluation tool for profitability of specific feed rations. Further, the study focuses on the possibility to cut feed costs via utilization of two by-products, HP-pulp and liquid stillage. Also, the study considers the significance of feed ration composition on feed strategy profitability.

The study aims to investigate financial effects originated from the employment of feed by-products. The impact on profitability is evaluated. Also, implications on resource allocation represent a core part of the thesis. A key feature of the study is the evaluation of implications for both production systems of the traditional dairy farm.

The theoretical perspective of the study bases in agricultural production economics. An adequate mathematical program is designed with basis in the work performed by Flaten (2001). It is complemented with research data and relationships from nutritional animal science to design the optimization model of the study.

This study employs a quantitative approach. The empirical work is based on existing data in the form of statistics. The statistics is utilized in the formation of the fictional case farms of the study. The objective of the study is to produce generalizable results that will serve as a guideline for farm managers in their cost saving efforts. The study employs an own developed mathematical model in the empirical work to give an example of an optimal behavior.

A key result is that the utilization of by-products has the opportunity to lower feed cost with 0,23 SEK per Kg ECM of produced milk. Which corresponds to an increased profit of 739 000 SEK per year in the case of a dairy farm with 300 cows and a production level of 10 000 Kg ECM on annual basis. Part of the saved cost originates from the production of feeds at farm level. A higher share of purchased is observed to lower operational cost of produced feeds since opportunity cost of grain production decreases. The phenomenon basis in re-allocation of farm resources from feed production to grain production.

The study recognizes that the competitiveness of employing feed by-products is dependent on the transportation distance from supplying plants. However, the study concludes that the utilization of by-products in the feed ration is likely to enhance profitability of feeding operations. Given a reasonable transportation distance, the employment of by-products has positive implications on both production systems of the dairy farm. Cost of the feed ration is reduced and grain production is expanded. However, a higher proportion of purchased feed leads to a more vulnerable situation for shifts in market conditions.

Sammanfattning

En ökad konkurrens på världsmarknaden för mejeriprodukter, samt ett svenskt mjölkpris som har hög korrelation med världsmarknadspriset har lett till svårigheter med lönsamheten för svenska mjölkgårdar. Detta skapar ett intresse för möjligheter att spara kostnader bland företagsledarna på mjölkgårdarna. Den dyraste utgiften i mjölkproduktion är kostnaden för foder. Således är studiens ämne kopplat till lönsamhet i foderstrategier för mjölkgårdar.

Studien fokuserar på att identifiera faktorer som påverkar det finansiella bidraget från specifika foderinsatser. Studien använder sig av utvärderingsverktyget mjölk minus foder för att på ett trovärdigt sätt utvärdera lönsamheten med en specifik foderstat. Mer specifikt försöker studien utvärdera möjligheten att spara foderkostnader genom möjligheten att utnyttja två biprodukter som foder, HP-massa och drank. Studien beaktar även foderstaters sammansättning av fodermedel och vilken betydelse det har för lönsamheten.

Studien syftar till att undersöka finansiella effekter av beslutet att använda sig av biprodukter i fodret. Vinstpåverkan av beslutet utvärderas. Påverkan på mjölkgårdens resursfördelning utvärderas också, vilket särskiljer denna studie från tidigare. Således är ett särdrag i denna studie att båda produktionsinriktningar på en traditionell mjölkgård undersöks samtidigt, i samspel med varandra.

Studiens teoretiska reflektion grundar sig i produktionsekonomi för lantbruk. En speciellt tillämpad matematisk modell är utvecklad med grund i det arbete som utfördes av Flaten (2001). Vilket i sin tur kompletteras med existerande data och samband från näringsvetenskap speciellt tillämpat för mjölkkor. Resultatet är en egenutvecklad optimeringsmodell som möjliggör studien.

Detta är en kvantitativ studie. Studiens empiriska undersökning grundar sig i existerande statistisk data. Dessa data används för att designa studiens fiktiva fallgårdar. Meningen med uppsatsen är att producera generaliserbara resultat som kan tjäna som riktlinjer för företagsledare i deras försök att spara in på foderkostnader. Studiens resultat ger exempel på rationellt beteende givet antagna förutsättningar.

Ett huvudsakligt resultat är att användning av biprodukter i foderstaten har potentialen att sänka foderkostnaden per producerad Kg ECM med 0,23 kronor. Vilket resulterar i en kostnadsbesparing med 739 000 kronor per år, givet en besättning på 300 kor och en medelavkastning på 10 000 Kg ECM. En del av kostnadsbesparingen grundar sig i en mer lönsam produktion av foder. Studien observerar att en högre andel inköpt foder leder till en lägre operationell kostnad för egenproducerat foder eftersom alternativkostnaden av spannmålsproduktion sjunker. Förklaringen är att gården allokera mer resurser från foderproduktion till spannmålsproduktion.

Studiens resultat bekräftar att konkurrenskraften av biprodukter som fodermedel är beroende av transportavstånd från fabrik. Dock finner studien att nyttjandet av biprodukter sannolikt förstärker lönsamheten associerad med foderarbetet. En huvuddel av studiens slutsatser inkluderar konstaterandet att nyttjandet av biprodukter har potentialen att förstärka lönsamheten i båda produktionsorienteringarna. Kostnader för eget foder reduceras och spannmålsproduktionen ökas. Dock leder en ökad andel inköpt foder till en mer utsatt position för marknadsförändringar.

Abbreviations and terminology

AAT – amino acids absorbed in the small intestine

DM – dry matter

ECM – energy corrected milk

GDT – Global dairy trade

Gsk – the production area of the forest districts of Götaland

Ha – hectare of land

IOFC – Income over feed cost

MFC – marginal factor cost

MP – multiparous (cows in a later lactation)

MPP – marginal physical product

NDF – neutral detergent fiber

PBV – balance of protein in the rumen

PP – primiparous (cows in first lactation)

VMP – value marginal product

“By-products” in this thesis denotes HP-pulp and liquid stillage.

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1 Introduction

Chapter one contains an overview of the current setting for dairy producers and attends the origin of the current situation. It displays the background to the research problem and basic conditions that determine the approach of the thesis.

The dairy sector has been struggling with varying profitability for a while. The price level of milk is volatile and to operate a dairy farm is a risky business due to present settings (LRF Mjölkk, 1, 2014; Debertin, 1986). The nature of a dairy firm makes it difficult to adapt to shifting market conditions. Since a majority of dairy farmers sell their milk to a dairy cooperative they only have a marginal scope of influencing price on their product. Thus the revenue stream is majorly affected by volume and partially by quality of the product. Consequently there is one viable direction left for profit improvement, rationalization of the cost structure (Debertin, 1986).

A manager in a dairy firm may however find some difficulties in the process of streamlining the cost structure. Most of the cost items in a dairy farm are the outcome from decisions made in earlier years. However the cost of feed is manageable in a somewhat shorter time period. Feed cost is also important to observe since it is the largest cost item in milk production (Buza et al., 2014). Hence feed strategy becomes an important part of operating dairy production in a profitable fashion. Some examples of decisions with impact on profitability of feed strategies are; farm grown feeds or purchased feed? Which crops to grow at the farm for feed purposes? Which feed products should be bought? Ultimately the mix of feed products determines the profitability of a feed ration, different feeds have different valuable attributes, and cost of acquiring the feeds (ibid).

One reason for the decreasing profitability Swedish dairy farmers facing is the internationalization of the market for dairy products. Arla is the biggest dairy cooperative in Sweden and as the market leader they have a high impact on the milk price faced by Swedish dairy farmers (internet, Arla, 1, 2015). Thus the Swedish milk price is highly correlated with the world market price of milk due to the transformation of Arla into an international dairy cooperative. Milk powder is the biggest export product of the Swedish dairy industry (SJV, 2012) and the world market price of milk is highly influenced by the price of milk powder on the Global dairy trade (GDT). GDT is a platform for online trading by the world's largest exporter of dairy products, Fonterra (internet, Fonterra, 1 & 2, 2015).

The current predicament for Swedish dairy farmers with financial stress is a result of a mismatch in global supply and demand. Europe has in years produced an excess of milk and has mainly exported dairy products to Russia and Asia where the production isn't enough for the domestic market (LRF Mjölkk, 2, 2014). In 2013 Russia introduced a trade embargo against the European Union as a response of the EU's sanctions against the country. The Russian trade embargo in combination with a decreasing demand, especially in Asia (LRF Mjölkk, 1, 2014) resulted in a considerably drop in the milk price on the GDT (internet, GDT, 2015). Furthermore the abolition of milk quotas within the European Union in May 2015 is posing a new threat to the Swedish dairy industry. It will likely lead to an increased production in countries producing at a level already exceeding the quotas (LRF Mjölkk, 2015).

Common for these countries are their conditions for milk production, which allow them to produce milk at a lower production cost compared to Sweden. The predicament of the Swedish dairy industry is now so grave that the government chose to act. A national plan of action to strengthen the profitability of the dairy producers has been developed during the spring of 2015 (internet, Government Offices of Sweden, 2015).

1.1 Problem background

A vital part of operating a competitive dairy farm is to employ a viable feed strategy (Buza et al., 2014). Two commonly appearing terms in this thesis are feed strategy and feed ration. It is important to understand the difference in order to avoid misinterpretations. Feed strategy is understood as an aware process of continuously evaluating market conditions in order to achieve a set mission (ibid). In this thesis the mission is profitability. Feed ration does simply refer to the actual composition of feed products.

It exists a few established regional markets for feed products based on residuals from the food processing industry (Nilsson, 2006; Slätt & Swensson, 2009). The market for these by-products is mainly limited to the southern part of Sweden. The two most promoted by-products are HP-pulp and liquid stillage. HP-pulp is supplied from Nordic Sugar's factory in Örtofta. Liquid stillage on the other hand is distributed from The Absolut Company's factory located in proximity to Åhus. The main decision factor for employment of by-products in the feed ration is the transportation distance from the distributing plants (Slätt & Swensson, 2009). Also these two by-products differs significantly in transportation cost for the same distance, since the dry matter of liquid stillage is low.

A qualified performance indicator to determine the profitability of a feed ration is income over feed cost, IOFC (Wolf, 2010). IOFC is popular as an evaluation tool because it relates revenue of produced milk to its largest expenditure. It is an advantageous tool since yield level in milk production is an outcome of amount and quality of feed, put into the cow.

Figure 1 illustrates differences in IOFC over the years 2006-2014. IOFC is often measured in relation to yield level. ECM stands for energy corrected milk, a standardization system to determine the content of one kilogram of milk. In December 2014 was IOFC 1,45 SEK/Kg ECM. It is a decrease of 0,70 SEK/Kg ECM compared to the situation for one year ago (LRF Mjolk, 2, 2014). It has however dropped to 1,30 SEK/Kg ECM in March 2015 (LRF Mjolk, 2015). Today it is remarkable if this remaining share of revenue is able to completely cover remaining cost items. Remaining expenditures include other variable costs in milk production, depreciation of equipment and buildings, wages, service and interest expenses.

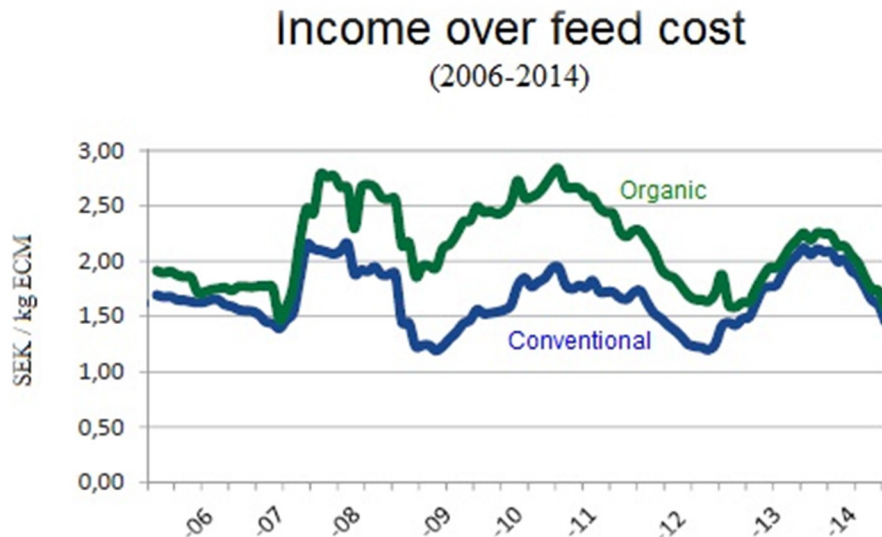


Figure 1. IOFC in Sweden during 2006-2014 (own modification of LRF Mjöl, 2, 2014).

Profitability of feeding strategies in dairy production is a widely studied area nationally as well as abroad. A common way in Sweden of conducting research within the subject is to focus on finding the most profitable composition of feeds using Norfor's feed evaluation system (Gustafsson et al., 2014). Norfor is the current standard system for feed evaluation within the Nordic countries and is used by scholars as well as feed advisors. A disadvantage of this method is that reliability of the results depends on the process of price estimation. Price estimation of products sold on a functioning market is not difficult, but to determine prices of feeds produced at farm level is imbedded with some difficulty. A similar approach is to investigate break-even prices of different feed products via Norfor's system (Gustafsson, 2012). This method lowers the uncertainty associated with the results. However it still excludes aspects of farm based feed production. This study uses a method that involves both crop and milk production as parts of the conventional dairy farm while assessing a theoretically correct price of forage.

A comprehensive study on feed strategies was made in the US (Buza et al., 2014). The study examines the effects of ration composition on profitability in dairy production. However the aim of the study was to investigate the profitability of observed feed strategies on existing farms. This method enabled the authors to form conclusions based on existing data. This study takes the opposite approach. Based on existing earlier studies and empirical data this study examines the most profitable feed ration in combination with resource allocation given certain conditions.

1.2 Problem statement

Profit maximization given alternative feed strategies is a complex problem with intertwined production systems, milk and crop production (Flaten, 2001). Furthermore, resource allocation has an impact on operational costs for intermediate goods. Further, a low milk price along with high grain prices, lead to a new reality for dairy producers. The situation creates a need for flexible feeding strategies to face volatile price levels in outputs as well as inputs.

1.2.1 Revenue maximization

A dairy farm has two main revenue sources with high correlation to feed strategy, sold milk and grain (Flaten, 2001). Milk however, is the largest commodity of a dairy farm and depends on quantity and variety of employed feed products. Thus, more and better feed increases milk production. Consequently, it also increases the cost of the feed ration. Produced grain can both be sold and used as feed (ibid). If produced grain is used for feeding purposes the farmer does not receive payment for it. This does not cause any revenue losses if milk revenue increases more than grain revenue decreases.

1.2.2 Cost minimization

Since feed cost is the biggest cost for milk production it is vital to minimize its extent (Wolf, 2010). This objective can be achieved in two manners. Either the farmer produces feeds at a low cost or purchase cheap feed products (Flaten, 2001). The choice between buying and producing feeds depends on which is more expensive, given that the two optional feeds have similar nutritional content. One course of action to acquire cheap feed products is to exploit the opportunity to use residuals from the food industry, feed by-products. Another aspect of minimizing feed costs is to strive for a feed ration composition with high efficiency (Buza et al., 2014). This means that the feed ration is designed in a fashion that utilizes the complementary qualities of different feeds in order to reduce required amount. Or in other words reduce waste in the feeding process due to over-feeding of expensive nutrients.

In summary, profit maximization problems have the dual nature of maximizing revenues and minimizing costs at the same time (Debertin, 1986). In the case of maximizing a dairy farm's profit with focus on feeding strategies the problem becomes even more complex. A chosen strategy has impact on profitability of two commodities. Allocation of more land to grain production leads to a possible increase in the expenses for acquiring feed (Svensson, 2013). Controversially a higher share of tillable land employed for feed production leads to decreased profitability of grain production. If a major part of the feed used is grown on the farm it reduces the need for buying marketed feed products (ibid). In conclusion the two production systems have to be economically evaluated collectively in order to constitute a valid decision support.

1.3 Aim

The aim of this thesis is to evaluate economic consequences of feed strategies in milk production at farm level. More specifically the study evaluates how the opportunity to use by-products in the feed ration affects the total profitability and income over feed cost for the milk. Economic consequences incorporate rational input use for profit maximization, which is conditioned by cost minimization of necessary costs like feed costs

The authors pose the following research questions to meet the aim:

- How does the opportunity to incorporate by-products in the feed ration affect total profit at farm level?
- How does optimal alternative feed strategies affect resource allocation at farm level?

1.4 Delimitations

The breed in focus of the study is Swedish Holstein, the most common breed in Swedish dairy production (internet, Svenskt kött, 2015). Other breeds are excluded from the study. Moreover breed management also falls outside the focus of the study. Another delimitation corresponding to the cow's anatomy is animal health aspects other than nutritional requirements, which to some extent are affected by feed ration. This study does not aim to find new results on the animal science field. The study is focused on a pure economic analysis of optimal feed strategies for the dairy cows.

The study do not take any consideration to risk preferences of the farmers due to significant variations and no opportunity to make a feasible assumption that reflects the average farmer (Flaten, 2001). The evaluation of by-products relative to general feed products is based on the assumption of no opportunities to utilize bargaining regarding the price of by-product feeds. Further the authors assume that increased demand does not affect prices of by-product feeds. The study is delimited to the southern part of Sweden. It is where most manufacturers of marketed by-product feeds are located (Nilsson, 2006; Slätt & Swensson, 2009). Large distances from the manufacturer increase the price of feed and subsequently affect a fair evaluation of the feed product's profitability.

To ensure that the results of the study are consistent, only one of the dairy cooperatives in Sweden is used as price reference. Arla is chosen because it is the largest dairy cooperative in Sweden and they publish their prices openly (internet, Arla, 2, 2015). No consideration is taken to variation in the demand for milk in Sweden with respect to season. The price of milk is mainly determined by international demand (LRF Mjolk, 2015). Thus, the milk price has no major impact on the possibility to answer the research questions. Furthermore the possible of quality variations in the milk commodity fall outside the scope of this thesis.

The topic of the thesis is feed strategies and the associated economic consequences. Thus hygiene aspects, feed handling processes and nutrient requirements with minor implications on feed ration design are disregarded, which may be argued to have an impact on profitability of the feeding strategy (Gustafsson et al, 2014). The reason is a need for a manageable empirical study with direct proximity to the field of economics. Consequently the flexibility of feed ration design is determined by the most significant technical feed requirement constraints in the model of this study.

To facilitate the profitability evaluation of feeding strategies based on IOFC the study has to focus on livestock in milk production. It makes the result of the study less generalizable since the method disregards feed consumption when breeding heifers within the herd. However, an attempt to capture the feed consumption of heifers would complicate the application of IOFC as evaluation tool (Wolf, 2010). In addition, the focus of the study is profitability of dairy production and heifer breeding is viewed as an investment.

All potential investment costs in feed storage are disregarded due to the nature of the research questions. The reason behind this position has two explanations (Bergknut et al., 1993). The first is the time perspective. This study has a short-term focus that does not enable a valid deduction of the implications on the operational cost of forage that originates in investment aspects. Moreover the results would be too determined by investment costs if they were incorporated in the empirical study. The second reason is that the environments surrounding

investment undertakings differ significantly between farms. Thus, the standardization prerequisite of the study does not hold if investment perspectives are incorporated in the empirical calculations (Robson, 2011). The model does not account for other costs than production costs of crops and feed purchasing costs related to the dairy cows. Hence, the thesis uses a concept of modified total profits, which with respect to the convenience for the reader is referred to as the total profit.

Possible environmental consequences of an altered feed strategy are not reflected in this study. The results of the study are not reflecting organic production, since legitimate production is determined through different frameworks (Patel, 2012). Moreover the study does not consider production conditions outside Sweden.

1.5 Outline

The outline of the thesis is presented in figure 2 below. It is a slight modification of the template provided for thesis writing. In chapter 1 detailed facts regarding the topic of the thesis is presented to form an awareness of the topic. The complementary facts are subsequently narrowed down in the process of formulating the aim of the study. The end of the chapter is providing information about the delimitations of the study. Chapter 2 provides an overview of earlier studies of interest of this thesis. In chapter 3 the theoretical framework is presented and adjusted to the subject of the thesis. This framework is later developed further into the model employed to answer the research questions of the study. In chapter 4 methodology considerations are presented. Here is also the work process of the thesis described in detail. Chapter 5 contains necessary parameter data for the mathematical model that enables the study. The chapter also contains descriptive information about the case farms of the study. This information provides the reader with a basic understanding necessary to comprehend the results presented in chapter 6.

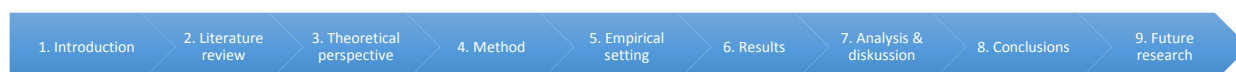


Figure 2. Illustration of the outline of the study (own illustration).

Chapter 7 entails both analysis and discussion. The analyses are carried out with regard to the theoretical framework. The discussion is based on findings in earlier studies, which are used in order to evaluate the authenticity and generalizability of the results. A presentation of the conclusions of the study is presented in chapter 8. The conclusions are based on the research questions formulated in chapter 1. The study finishes with chapter 9 and contains suggestions of some future research topics and areas, which relate to the findings in this thesis.

2 Literature review

The object of this chapter is to provide an overview of earlier studies conducted within the field of feed strategies in the dairy sector (table 1). Furthermore, this chapter offers the reader a basic understanding of research conducted within the topic of the study. Hence, the chapter illustrates a researcher's methodology options and serve as decision support for narrowing down the aim of this study.

2.1 Earlier studies within the topic

The common subject of the following studies is the aspect of profitability in dairy production. They however differ in methodology and focus within the production process.

2.1.1 Studies with a general focus on profitability aspects in dairy production

A study performed by Svensson (2013) is based on fictional case farms to enable a simulation methodology. The aim of the study is to examine if geographical locations of Swedish dairy farms have impact on chosen feed strategies and the financial results attached. Svensson concludes that regions with limited conditions for competitive crop production has reduced opportunity cost for farm grown feeds. A recently conducted American study uses real case farms to explore the impact of feed ration composition on dairy farm profitability (Buza et al., 2014). One essential conclusion of the study is that a lowered share of forage in the feed ration has a positive effect on financial outcome. The authors also suggest that utilization of by-products has potential to enhance farm profitability. Wolf (2010) performed another American study on the subject of managerial tools in dairy production. Wolf uses a statistical analysis to examine economic evaluation tools employed in dairy production management. The main conclusion of the study is that income over feed cost, IOFC, is the most comprehensive and accurate management tool for investigating profitability attached to a specific feed ration.

2.1.2 Studies with the focus of feed ration aspects

A number of studies with the topic of feed ration profitability are conducted via Norfor's feed evaluation system (Gustafsson et al., 2014; Slätt & Swensson, 2009). Norfor is the latest and most advanced program for evaluation of the profitability attached to employing specific feed products in the feed ration (Lärn-Nilsson, 2007). Gustafsson (2012) uses Norfor to evaluate economical break-even points for feed products for dairy cows. A similar study also conducted in Sweden, uses a simulation methodology to compare the financial competitiveness different protein feeds (Gustafsson et al., 2014). The focus is to evaluate protein feeds produced in Sweden as an alternative to the imported protein feeds that currently dominate the protein feed market (ibid). The authors conclude that given the right circumstances the utilization of Swedish protein feeds may be financially viable. Another study employs the Norfor model to investigate the profitability attached to utilizing liquid stillage feed in the feed ration (Slätt & Swensson, 2009). The result of the study implies that liquid stillage is a competitive feed alternative given a maximum distance of 20 Swedish miles to the distributing plant in Nöbbelöv, located in southern part of Sweden.

Table 1. Overview of previous research conducted within the topic (own illustration).

Earlier studies	Subject of the study	Method	Country
Alvemar, 2014	Controlled traffic farming (CTF) in forage production for dairy cattle.	Mathematical programing	Sweden
Andersson & Gotting, 2011	Comparison of competitiveness between the dairy sectors of Sweden, Denmark and Germany.	Mathematical programing, linear programing	Sweden
Buza et al., 2014	Investigate profitability of observed feed strategies on real case farms.	Real farm case study	USA
Flaten, 2001	Economic analysis of Norway's dairy producers.	Mathematical programming, linear programing	Norway
Freeze & Richards, 1992	Estimation of lactation curves.	Modelling, simultaneous equation model	Canada
Gunnarsson, 2002	Evaluation of economic aspects of the introduction of VMS.	Mathematical programming	Sweden
Gustafsson, 2012	Finding break-even prices of different feed products.	Economic calculation with Norfor	Sweden
Gustafsson et al., 2014	Economic evaluation of different feed strategies from Norfor.	Simulation study with Norfor	Sweden
Klein et al., 1986	Optimization model for feed concentrate use in dairy production.	Mathematical programming, linear programing	Canada
Nygren, 2010	Analyzed how daily feed ration calculations affect the feed costs.	Mathematical programming, linear programing	Sweden
Patel, 2012	Study economic effects of high forage rate in feed ration.	Experimental, Calculations	Sweden
Slätt & Swensson, 2009	Economical examination of utilizing liquid stillage as feed.	Feed ration optimization with Norfor	Sweden
Svensson, 2013	Evaluation of economic value of farm based feed production.	Simulation, case study	Sweden
Wallman et al., 2010	Feed strategies' environmental impact and costs.		Sweden
Wolf, 2010	Validation examination of different economical evaluation tools for dairy farm management.	Calculations, statistical analysis of existing data.	USA

Another aspect of feed ration composition is the environmental impact associated with dairy production. One study explores environmental consequences of different feed strategies applied in Swedish dairy production (Wallman et al., 2010). A study performed by Patel (2012) investigates emissions associated with feed strategy choices. The specific aim of the study is to examine differences in the share of forage employed in the feed ration, how it affects emissions and implications on profitability. The authors conclude that a high share of forage in the feed ration increases the environmental footprint.

2.1.3 Studies using the optimization methodology

One of the most common methods to investigate feed strategy profitability is the employment of an optimization model (Flaten, 2001; Gunnarsson 2002; Andersson & Gotting, 2011). Flaten (2001) conducted a comprehensive study via development of a well-recognized optimization model for dairy production. His aim was to explore Norway's general conditions to uphold a competitive dairy production. This model occurs in a number of later studies (Gunnarsson 2002; Andersson & Gotting, 2011). The study performed by Gunnarsson (2002) utilizes Flaten's optimization model to explore economical outcomes of an investment in DeLaval's VMS technology concerning the Swedish conditions. Andersson & Gotting (2011) further customize Flaten's model to investigate the relative competitiveness of dairy farmers in Sweden, Denmark and Germany.

Freeze & Richards (1992) estimated lactation curves for Canadian Holstein to use in mathematical programming. Nygren (2010) later employs one of these lactation curves. Nygren performs an analysis of feed costs in dairy production with focus on daily feed ration calculations and the effects of overfeeding. He concludes that the cost of overfeeding increases with the employment of complete diet feed rations. Another study built a linear programming model aiming to maximizing the farm level profit for dairy cattle. The authors' objective was optimization of concentrate feed employment (Klein et al., 1986). A recent Swedish study by Alvemar (2014) uses results from field trials in an integer programming model to determine the competitiveness of controlled traffic farming, CTF, in forage production. Alvemar concludes that CTF has the potential of lowering operational cost for forage through an increased yield level in forage production.

2.2 Summary

In summary, feed costs in dairy production are a frequently occurring research topic. The reason seems to be technological development and increasingly tougher competition on the world market (Gustafsson et al., 2014). This in a setting there increasing political regulation requires environmental considerations.

A number of studies within the topic are conducted via an optimization model. This method gives a clear view of the most rational behavior. However, the method gives a snapshot solution and does not capture the whole picture of shifting market conditions. An alternative method is simulation, which sets up a number of likely situations and calculates associated financial outcomes given specific conditions (Svensson, 2013). The method is appropriate to illustrate how certain conditions affect the possibility of competitive dairy production. This thesis however on the contrary aims to provide the reader with guidelines for rational behavior in shifting market conditions to maintain financial edge. Another occurring method

for examining competitiveness of different feed products is to calculate break-even prices of current production conditions (Gustafsson, 2012). Yet, the method does not provide information about impacts of shifting market conditions.

The authors observe a missing research area where previous studies lack a full reflection of the complex decision process attached to feed strategy choices. It is common to assign farm grown feeds with a price based on statistics (Gustafsson et al., 2014). This approach to the problem enables a focus on solely dairy production with associated feed costs. However, the price deduction of farm based feed production in this fashion has a certain degree of uncertainty (ibid). Moreover, this method for price deduction does not incorporate shifting market conditions that should have an impact on pricing of intermediate goods.

Hence, the authors sense a need for an optimization model that considers the dual production of the dairy farm as feed strategy choices affect both production systems. Deduction of operational cost of farm grown feeds is a well-recognized approach to consider the link between the production systems (Andersson & Gotting, 2011). This price deduction method enables an illustration for the impacts of shifting market conditions. Thus, the dairy farm manager is provided with reliable decision support in the process of forming a competitive feed strategy. However, it is important to remember that foregone revenue considered in operational cost is not equal to an actual payout.

3 Theoretical perspective

In this chapter theories that represent the basis for developing the study's empirical model are presented. The study considers theories regarding production economics, optimization, and investment appraisal.

The theoretical foundation of the study is represented by classical microeconomic theory (Pindyck & Rubinfeld, 2009). Microeconomics' core area is behavior of individual economic entities. More specifically it deals with market players' economic decision-making. Actors strive to maximize utility, which often is equalized to profit maximization (Debertin, 1986). The permanent problem for any firm manager is to allocate scarce resources in a profit maximizing fashion. The manager's behavior is dependent on the production function of the commodity as well as prices on inputs and outputs.

3.1 Production function

An important management tool is the concept of production function, which describes how inputs are consumed in relation to the commodity produced (Debertin, 1986). Information given by the production function is necessary in order to maximize profit. The production function possesses information about each input's contribution to assembling the product. This relationship in correlation with input price and commodity price give information about how resources should be allocated to a specific production activity. The general expression for the production function is presented in equation (1).

$$y = f(x) \tag{1}$$

The production function expresses output level, y , as a product of input amount, x . This expression is valid for any value of x equal to or exceeding zero, which provides a value for y . However equation (1) is the most simplified expression of a production function (Debertin, 1986). Few firms display a production function where a commodity only uses one resource in production. Nevertheless the theoretical implications of the general expression are still valid for far more complex production functions. Another general expression for a more comprehensive illustration of the production function is represented by equation (2).

$$y = f(x_i|u_i) \tag{2}$$

This function introduces a distinction between variable input, x_i , and fixed input, u_i . An example of a variable input in dairy production is feed (Flaten, 2001). On the other hand buildings and land often fall under the fixed input category. The distinction between variable and fixed inputs is dependent on the ability to alter employed amounts (Pindyck & Rubinfeld, 2009). A variable input is traditionally categorized as an input that is manageable in volume when facing shifting market conditions. In contrast, the manager is normally unable to alter the amount of fixed resources employed. However the distinction does also relate to a time perspective. If enough time passes approximately all resources become variable. Yet dairy farmers act on a market with highly volatile prices (ibid). This environment reduces the opportunities for proactive planning. Hence a major portion of the cost of a dairy farm is traditionally viewed as fixed costs.

A vital aspect of the production function is the law of diminishing returns (Debertin, 1986). This means that inputs differ in efficiency in terms of transforming into outputs at different production levels. One way of displaying this phenomenon is to calculate the marginal physical product (MPP) of an input. It means to what extent an additional unit of input contributes to producing one more unit of the output, consequently this measure relates to a certain production level (ibid). Another aspect of the phenomenon is to attach MPP to the commodity price, which gives the value marginal product (VMP). This measure reveals how expended inputs contribute to revenue streams. At a certain level of production the profit maximizing level of production is reached (ibid). At a lower level of production the firm enhances profits if they increase production and vice versa. The profit maximizing level of production also depends on marginal factor cost (MFC). MFC is equal to the input price if the farmer is unable to utilize discounts when purchasing marketed inputs. The profit maximizing level is reached when VMP is equal to MFC (ibid).

Given a company with a production function containing more than one input, the manager has to consider substitution among inputs (Pindyck & Rubinfeld, 2009). The principal determinant for input choice is input price if two inputs have a similar contribution effect in production, in other words they are categorized as substitutes. Another aspect of input choice is the technical complementary effect between inputs (Debertin, 1986). Inputs are viewed as technical complements if an increase in the amount of one input enhances the productivity of another input.

3.2 Profit maximization

Profit maximization has two different dimensions, revenue maximization and cost minimization (Debertin, 1986). The objective is accomplished when the firm identifies the production level where these dimensions are combined. The general expression to denote profit maximization is presented in equation (3).

$$\begin{aligned} \max \pi &= P_y * y - P_x * x_i - FC & s. t. & y \leq f(x_i|u_i) & (3) \\ & & & y \geq 0 & x_i \geq 0 & u_i \geq 0 \end{aligned}$$

Profit is denoted by π and is dependent on total revenues and total cost. Total revenues are determined by price of the commodity, P_y , and the quantity produced, y . Total costs on the other hand consist of two entities; one variable and one fixed (Debertin, 1986). The variable cost is determined by the price of the input, P_x , and the amount of employed input, x_i . Fixed cost is denoted by FC and is not correlated to level of production.

A more comprehensive approach to profit maximization is to ensure maximized output from employed inputs (Debertin, 1986). The expression for this mindset is formulated in equation (4).

$$\max \pi = P_y * f(x_i) - P_x * x_i - FC \quad (4)$$

To enable the development of theoretical model for profit maximization of a typical dairy producer, three criteria have to be fulfilled (Flaten, 2001): 1st, the problem has to consist of a continuous and identifiable production function. 2nd, divisibility in the relationship between

inputs and outputs. 3rd, the relationship expressed in the production function might be homogenous to the degree of one.

To sustain a long-term profitable production the revenues of an employed input has to be larger than the cost, $P_y f(x) > P_x x + FC$. The expression can also be rewritten as:

$$P_y > \frac{P_x x + FC}{f(x)} \quad (5)$$

Equation (5) illustrates the general expression for long-term profitability in production (Flaten, 2001). The objective is achieved when the commodity price exceeds the average production cost per unit, AC. Still in the case of financial distress, it would be economically viable to operate production as long as the output price covers the variable costs, AVC; $P_y > \frac{P_x x}{f(x)}$. The surplus from production does in this case cover some part of the fixed costs, which appears regardless if production is running (Flaten, 2001). Thus this course of action limits the losses even if revenues drop.

The derivative from equation (4) has to be calculated in order to identify the profit maximizing production level (Debertin, 1986). The first order necessary condition, FONC, is calculated by partially differentiating the equation (4) with subject to x_i . The FONC contain information about the optimal use of an input. Moreover it expresses how profit changes if one additional unit of input x_i is added. The FONC is normally formulated as:

$$\frac{\partial \pi}{\partial x_i} = P_y f'(x_i) - P_{x_i} = 0 \quad (6)$$

Equation (6) illustrates that the optimal input use is not restrained by FC (Flaten, 2001). A simplified expression of the relationship is:

$$P_y MPP_x = P_x \quad (7)$$

Equation (7) demonstrates the condition for the resource allocation either when minimizing costs or maximizing profits (Debertin, 1986). To meet the condition does not reveal which extreme the production level results in.

3.3 Profit maximization for a dairy producer

So far the basic theory for profit maximization in firms are explained. However the profit maximizing equation (4) has to be more detailed to highlight the special conditions facing a dairy farmer (Debertin, 1986). Equation (8) illustrates the revenue and cost streams of a typical dairy firm, although still in a simplified state to cover the theoretical base of the study.

Profit as concept is determined by the summary of revenues that is subtracted for cost items (Pindyck & Rubinfeld, 2009). The major part of a dairy farm's revenues consists of return from sold milk (Debertin, 1986). This is illustrated in equation (8). Still some revenues proceed from grain production relying on feed requirements already being met. The farmer has the option to purchase grain from crop growing farmers. The trade balance is indirectly visible in the second entity of equation (8) and is a key component if the farmer both grows

and purchases grain. Other marketable commodities produced at a dairy farm fall outside the scope of this thesis since they theoretically are unaltered by feed strategies.

The major cost item is feed acquirement, which can be conducted in two fashions. Feed may be produced at the farm or purchased as commercial feed products. In crop production the available land may be used for growing forage or grain (Flatén, 2001). While grain crops may be sold as commodity, grown forage is only used as feed due to the lack of a functioning market.

$$\max \pi = P_y f(X_k, X_g, X_a)N + P_k(A_k Y_k - N X_k) - C_k A_k - C_g A_g - P_a N X_a - FC \quad (8)$$

$$N, X_k, X_g, X_a, A_k$$

$$\text{s.t.} \quad A_k + A_g \leq \bar{A} \quad NX_g = A_g Y_g$$

$$N(e_k X_k + e_g X_g + e_a X_a) \geq \bar{E}$$

The profit function (8) is also restrained by some constraints since the farmer's way of conducting business is determined through the employment of restricted resources. The two major constraints a dairy farmer faces are; available land and nutritional requirements for milk production.

N	=Number of cows in production
P_y	=Milk price
$f(K_i)$	=Production function for milk production
P_k	=Price of feed grain per Kg DM
P_a	=Price of feed by-products per Kg DM
A_k	=Land for grain production
A_g	=Land for forage or silage production
Y_k	=Yield of grain production, kg per ha
Y_g	=Yield of forage or silage production, kg per ha
X_k	=Kg of feed grain per cow
X_g	=Kg of forage or silage per cow
X_a	=Kg of feed by-products per cow
FC	=Total fixed costs
\bar{A}	=Total land
e_k	=Nutritional supply of one Kg DM of feed grain
e_g	=Nutritional supply of one Kg DM of forage or silage
e_a	=Nutritional supply of one Kg DM of feed by-products
\bar{E}	=Total nutritional requirement
λ_1	=Shadow price of land
λ_2	=Shadow price of nutritional requirements
P_g	=Operational cost of forage or silage produced per Kg DM

3.4 Lagrangean function

In order to enable the mathematical programming approach of this study a Lagrangean function has to be formulated. The Lagrangean function embraces the complex nature of a profit maximization problem in the case of scarce resources (Debertin, 1986). A Lagrangean function includes a mathematical expression for the implications of fixed volume of key resources. The impact of these restrictions on the farms profit is expressed by λ , Lagrangean multiplier or shadow price, which states the marginal cost, MC, of the fixed resource volumes at specific production levels (ibid). If the shadow price, $\lambda = 0$, it entails that the restricted amount of the resource is sufficient. In other words the quantity available does not affect profit negatively. In opposite, when the constraint is binding, the shadow price expresses how profit differs if the resource quantity is altered with one unit.

$$\begin{aligned} \max L = & P_y f(X_k, X_g, X_a)N + P_k(A_k Y_k - N X_k) - C_k A_k - C_g \frac{N X_g}{Y_g} - P_a N X_a - FC + \\ & \lambda_1 \left(\bar{A} - \frac{N X_g}{Y_g} - A_k \right) - \lambda_2 [\bar{E} - N(e_k X_k + e_g X_g + e_a X_a)] \end{aligned} \quad (9)$$

Equation (9) is an extension of equation (8). In the equation (9) A_g is substituted with $\frac{N X_g}{Y_g}$ in agreement with the condition mentioned in the mathematical scheme presented alongside equation (8). When it is transformed to a Lagrangean function the total available amount is added as well as the nutritional requirement aspect. Equation (9) is maximized with subject to seven variables determining the profit, $N, X_k, X_g, X_a, A_k, \lambda_1, \lambda_2$. In the current case the farmer faces two constraints that yield two shadow prices. The formulated Lagrangean function allows for calculations of the FONC's, which reveal the sensitivity of the variables exposed to the restrained resources. The calculations of the FONC's are presented in equations (10-16):

First order necessary conditions for the current case:

$$\frac{\partial L}{\partial N} = P_y f(.) - P_k X_k - \frac{C_g X_g}{Y_g} - P_a X_a - \frac{\lambda_1 X_g}{Y_g} = 0 \quad (10)$$

$$\frac{\partial L}{\partial X_k} = P_y f'_{X_k} (.)N - P_k N + \lambda_2 N e_k = 0 \quad (11)$$

$$\frac{\partial L}{\partial X_g} = P_y f'_{X_g} (.)N - \frac{C_g N}{Y_g} - \frac{\lambda_1 N}{Y_g} + \lambda_2 N e_g = 0 \quad (12)$$

$$\frac{\partial L}{\partial X_a} = P_y f'_{X_a} (.)N - P_a N + \lambda_2 N e_a = 0 \quad (13)$$

$$\frac{\partial L}{\partial A_k} = P_k Y_k - C_k - \lambda_1 = 0 \quad (14)$$

$$\frac{\partial L}{\partial \lambda_1} = \bar{A} - \frac{N X_g}{Y_g} - A_k = 0 \quad (15)$$

$$\frac{\partial L}{\partial \lambda_2} = -[\bar{E} - N(e_k X_k + e_g X_g + e_a X_a)] = 0 \quad (16)$$

Equation (11) and (12) can be rewritten as:

$$P_y f'_{x_k}(\cdot) - P_k + \lambda_2 e_k = P_y f'_{x_g}(\cdot) - \frac{c_g}{Y_g} - \frac{\lambda_1}{Y_g} + \lambda_2 e_g \quad (17)$$

Equation (12) and (13) can be rewritten as:

$$P_y f'_{x_g}(\cdot) - \frac{c_g}{Y_g} - \frac{\lambda_1}{Y_g} + \lambda_2 e_g = P_y f'_{x_a}(\cdot) - P_a + \lambda_2 e_a \quad (18)$$

Equation (11) and (13) may then be rewritten as:

$$P_y f'_{x_k}(\cdot) - P_k + \lambda_2 e_k = P_y f'_{x_a}(\cdot) - P_a + \lambda_2 e_a \quad (19)$$

Simplifying equation (17) yields:

$$\frac{P_y MPP_{x_g}}{P_y MPP_{x_k}} = \frac{\frac{c_g + \lambda_1}{Y_g} - \lambda_2 e_g}{P_k - \lambda_2 e_k} \quad (20)$$

Note that: $\lambda_1 = P_k Y_k - C_k$ and equation (7): $P_y MPP_x = P_x$

Through equation (20) it is possible to deduce the operational cost of forage. Due to lack of market the feed has to be priced in line with each farm's cost structure and available resources. Accordingly the operational cost of forage is: $P_g = \frac{c_g + \lambda_1}{Y_g} - \lambda_2 e_g$. The cost of production depends on the variable costs associated with production as well as the yield. It is also determined by the opportunity cost of not being able to grow grain on part of the land, λ_1 . This leads to more expensive roughage in geographical territories associated with competitive grain production. Finally forage's operational cost is subject to the ration of forage per cow and the unbreakable nature of the feed requirement constraint, λ_2 .

Simplifying equation (18) yields:

$$\frac{P_y MPP_{x_g}}{P_y MPP_{x_a}} = \frac{\frac{c_g + \lambda_1}{Y_g} - \lambda_2 e_g}{P_a - \lambda_2 e_a} \quad (21)$$

Simplifying equation (19) yields:

$$\frac{P_y MPP_{x_k}}{P_y MPP_{x_a}} = \frac{P_k - \lambda_2 e_k}{P_a - \lambda_2 e_a} \quad (22)$$

The arrangement of the expressions in equations (20-22) entails information about price ratios between the main categories of feeds. These ratios are important in the process of forming an economically viable feed ration. The range of options in combining different portions is however still subordinated to technical prerequisites expressed in the nutrient requirement constraint.

4 Method

This chapter contains information about the execution of the study. Chosen methods are explained and their adequacy are interpreted. Possible complications that originate from the choice of method are discussed and ethical issues are considered.

4.1 Methodological approach

This section is meant to highlight the issues of methodology choice in the process of conducting the study. This is an explanatory section with motivation for the methods of choice.

4.1.1 Research design and strategy

Traditionally social science research has been conducted in one of two alternatives, quantitative or qualitative research (Bryman, 2008; Robson, 2011). The quantitative method has been developed as an attempt to mimic traditional ways of carrying out natural science research. The qualitative method originates from the idea that individuals, personal interaction and social settings are central aspects of social research. Since these strategies traditionally are rather static in their approach and methodology they have been subject to extensive criticism (Robson, 2011). Another alternative is to use a mixed research method, where quantitative and qualitative approaches are combined. Depending on the research aim a mixed method can either be synergetic or troublesome, because the two research traditions are highly polarized in terms of aspect regarding design strategies.

The study is conducted with a quantitative approach since the larger part of the empirical data collection consists of numerical data gathering which is used in the optimization model in order to answer the research questions. The quantitative method enables some degree of generalization. The generalization is about finding data that makes the optimization applicable to larger size farms with similar conditions, not to reflect the average farm in the region. Personal messages are used to validate gathered empirical data used in the model. These unstructured interviews allow the authors to gather essential technical and biological data requisites.

4.1.2 Modeling decision making

In the process of conducting quantitative research it is imperative to select an appropriate type of model to work with. In the case of this thesis the objective is to find a model that to a significant extent mimics the decision process the farmer faces in reality. It exists two orientations within the field of decision models, descriptive and normative (Turban et al., 2001). They are both based on mathematical relationships. The most common descriptive model is simulation (Anderson et al., 2014). It is a method developed with the focus to mimic the reality with high accuracy. In brief, simulation is a method to forecast the consequences of a decision alternative. An advantage with simulation models is the generation of a more comprehensive understanding of the problem, due to fewer simplifying assumptions about the reality (Turban et al., 2001). However the outcome of a decision made by the assistance of a simulation model is not equivalent to the best decision alternative. It is often said that it may

compute a satisfactory decision alternative, while it may overlook a better alternative since it does not take all possible alternatives into consideration.

The normative model is an attempt to compute a model that generates the best decision alternative (Turban et al., 2001). The best decision alternative implies that all other possible alternatives would be less preferable. A normative model is often referred to as optimization and entails an optimum allocation of scarce resources to meet set objectives. The optimization problem takes the form of either a minimization or a maximization problem (Anderson et al., 2014). Normative modeling entails three assumptions about the rational decision maker, henceforth also mentioned as the manager (Turban et al., 2001). The manager is always maximizing utility with basis in firm objectives. The decision maker has the ability to estimate all possible consequences of decision alternatives and rank them appropriately based upon desirability. These assumptions have however been the object of extensive criticism. Critics raise concerns about the irrational nature of the human and the wearing circumstances that decision makers face (ibid).

To answer the first research question, a descriptive simulation would be sufficient but in order to answer the second research question a normative model is indispensable. The optimization enables the possibility to reallocate resources freely within given frames in an optimal manner which the simulation cannot do.

4.1.3 Case study research

The case study enables the opportunity to compare different scenarios without considering all details of a case (Ejvegård, 2009). By using case studies of fictive farms, the thesis isolates the influencing variables and may delimit variables of less importance to the research questions. Case studies can be conducted in many ways, as a study of a single case or different kinds of multiple case studies (Robson, 2011). A multiple case study enables results which may be replicated and analytically generalizable but not necessary statistically reliable (Yin, 2003).

A central part of the study is based on comparison, between outcomes from the case farms. Another aspect is the comparability of the input factors in the optimization model. In comparisons the following criteria must be fulfilled (Ejvegård, 2009):

- Ensure that the data is comparable to another,
- Before starting the comparison, make necessary generalizations,
- Transfer all data into the same units and make necessary corrections for differences in data collection,
- Describe both differences and equalities.

The need to fulfill these criteria was central in the choice of fictive case farms instead of using real farms in this study.

4.2 Literature review

The literature review is used to find adequate prior studies conducted within the topic of the thesis. Suitable theories are identified to form a collaborative base for development of the

model. Earlier studies are also used to precisely define phenomenon which must be considered and which are not influencing the specific research questions. The literature review is mainly based on peer-reviewed primary sources in order to maintain a satisfactory reliability. In the case where secondary sources are used, it is in the form of acknowledged textbooks in respective fields. Material in the literature review is gathered from books, theses, scientific articles, scientific journals and dissertations. The main area to collect material regards aspects of the cow's lactation process and the nutritional requirements for producing milk. The focus has been the unique conditions for conducting dairy production in Sweden. These findings are subsequently complemented with more general conditions from the rest of the world to enable a more comprehensive understanding of the topic.

The process of conducting the literature review is performed through the assembling of a series of keywords. They are utilized to collect material from a number of databases provided by the Ultuna library. Used databases are: Primo, Google scholar and Web of science. A sample of important keywords that cover the main area is: dairy production, milk production, lactation period, lactation curve, cow nutrition, nutritional requirements, feed values and feed production. The databases contain a wide range of academic material and are a useful tool to access papers that are published at SLU as well as external.

One essential element in a literature review is to examine used sources. Otherwise the reliability of the process risks to be compromised and the error margin in the analysis of the result increases. Due to the nature of this study, validation and comparison of sources is crucial for reliable results. To validate the trustworthiness of the sources used it exists four quality parameters to consider: authenticity, time conjunction, independency and tide liberty, (Thurén, 1997). With these quality parameters in mind, all employed sources of the thesis is scrutinized.

The literature review fulfills two essential objectives in this thesis. One is to ensure the relevance of the study that is presented in chapter 2. The other objective is to provide the model making process with critical information and data, which is presented in chapter 5.

4.3 Applied optimization

This section highlights important considerations of applied optimization as method of conducting a study. It raises advantages of the methodology, specific disadvantages and raises considerations thereof.

4.3.1 Linear programming

Within optimization the problem can appear in two forms, linear and nonlinear (Debertin, 1986). A linear problem consists of merely linear elements. The nonlinear optimization problems consist of at least one non-linear component, in either objective function or constraints. However, linear programming has a wide range of applications within nonlinear problems (ibid). This is true in the case of the agricultural sector where cost and production functions seldom appear as linear. In the case of this study the authors apply linear programming. This is possible since the nature of the nonlinear elements of the problem do not express relationships in either objective function or constraints. The nonlinear

relationships only refer to value calculations of technical prerequisites that form the constraints of the study.

Linear programming enables a possibility to investigate the best decision alternative for allocating scarce resources in a mixture problem, e.g. feed ration composition and crop allocation. Three control requirements are stated to ensure applicability of linear programming (Hazell & Norton, 1986): 1st, all conceivable farm activities and their resource consumption must be identified. Also the restrained supply of resources regarding the employment of a certain activity needs to be formulated into constraints, e.g. nutritional requirement for milk production. 2nd, level of vacant resources need to be specified, e.g. barn capacity and available land. 3rd, the contribution value of activities need to be calculated accurately. This in order to denote profit alteration attached to activity employment.

If these conditions are fulfilled the linear programming method produces a valid result (Hazell & Norton, 1986). The next step is to formulate the objective function of the problem, which in the case of the study is maximized. The objective is to maximize the profit of all farm operations. The general form of a profit maximization problem is expressed in equation (23) (Pidd, 2009):

$$\pi = \sum_{j=1}^n c_j x_j \quad (23)$$

As illustrated in equation (23) π denotes profit of the farm (Hazell & Norton, 1986). C_j expresses the contribution value of employing one unit, x_j of activity, j . To calculate total profit the contribution values of employed units to activities are summarized. The contribution value of each activity is either positive or negative. The problem formulation is valid for any amount of j and allows for any number of different activities. However a condition for applying linear programming is that x_j is not allowed to take a negative form, stated in equation (24). Finally the objective function cannot in reality be unconstrained due to restrained supply of resources (Pidd, 2009). Consequently is the general form of a constraint expressed in equation (24):

$$\begin{aligned} \sum_{j=1}^n a_{ij} x_j &\leq b_i, & i &= 1, \dots, m. \\ x_j &\geq 0, & j &= 1, \dots, n \end{aligned} \quad (24)$$

In short does the mathematical expression in equation (24) state that resource consumption cannot exceed the available amount (Hazell & Norton, 1986). The resource consumption of activity j for employing one unit of x_j is denoted by a_{ij} . The available amount of resource i is indicated by b_i . Different resources consumed by activity j are represented by i and can be numerous. The relationships hold given the condition that resource consumption is nonnegative and the level of amount employed, x_j , is also nonnegative.

4.3.2 Sensitivity analysis

As mentioned earlier is the optimization approach an attempt to find the best course of action in a decision situation. However, the solution given by the optimization model is only true for a snapshot of the reality (Lundgren et al., 2001). Moreover if there is uncertainty correlated to data gathering the optimal solution is questionable in reliability. These obstacles have created a need for complementary information regarding the solution, also labeled a sensitivity analysis (ibid). The sensitivity analysis is meant to test the robustness of the solution and is often an equally essential decision support as the solution. Since agricultural firms act in a changing environment the comprehensive information given by the sensitivity analysis is important to choose the appropriate course of action. Through a sensitivity analysis it is possible for the decision maker to identify the factors that are most risky and which affect the outcome the most. A sensitivity analysis may also prove helpful to identify the break-even point, the situation when an investment is financially feasible.

A sensitivity analysis can be created manually through changes in important decision variable, e.g. costs, prices, expenditures and demand (Lundgren et al., 2001). It is although only possible to alter one value at the time in the sensitivity analysis. Hence a sensitivity analysis is not really that comprehensive as advocates proclaim. If the optimization is executed in the computer program Excel, the program constructs a sensitivity analysis regarding the situation at hand (Pidd, 2009). A condition for Excel to be able to create a sensitivity analysis is that the optimization problem does not take the form of integer programming. In this study integer programming is not applied, which leads to that Excel computes a sensitivity report but a manual sensitivity analysis of important variables is also conducted.

A key feature of a sensitivity report produced by Excel is the shadow prices, which correlate to each binding constraint (Pidd, 2009), see section 3.4. The shadow price expresses how profit is affected by a change in the amount of available resources (Debertin, 1986). If constraints are classified as amount of resource or technical prerequisite in production the shadow price serve different purposes as decision support. A high shadow price is the result of a situation where a key production input is too restrained (ibid). Thus the shadow price reveals the farmer's willingness to pay for obtaining the appropriate amount to maximize profit. This holds as long as technical conditions for production remain unaltered by investments in productivity. A shadow price of technical prerequisites may serve as an evaluation tool for future investments in increased productivity.

4.4 Empirical study

This section explains how and why the empirical part of the study is conducted in the chosen fashion. This study generates the empirical results by optimization of data based on own modeling, statistics and use of secondary data from the field of animal science. To develop a model, the complex real world situation must be simplified. This is illustrated in a schematic overview (figure 3). The next step is to isolate the central elements that have major impact of the outcome related to the research questions. The model is then structured around these elements in a manner that focuses on answering the posed research questions.

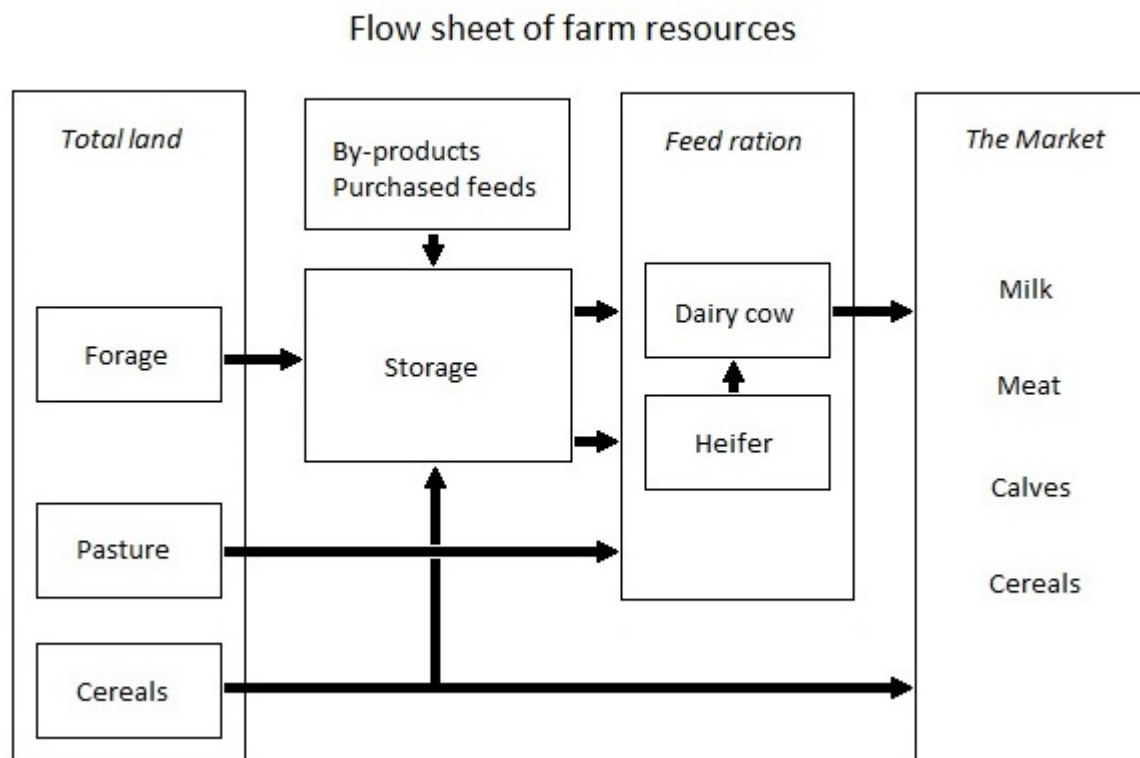


Figure 3. Overview of farm resources (own modification of Ekman, 1995).

The optimization is conducted on three fictional case farms, where the geographical location is the only difference. The location is central to the outcome of the empirical study and thus the answer of the research questions. A fourth farm without opportunity to utilize HP-pulp and liquid stillage is used as reference. This reference farm is central due to the comparative nature of the research questions. The reference farm represents the “no by product” scenario of each case farm due to the identical conditions for the three case farms with exception for the geographical location.

The optimization of the case farms is based on empirical data validated according to the principles explained in previous section in order to answer the research questions. The maximization problem is defined on total farm level, which implies that the model optimizes all farm level operations. The outcome of the total profit maximization is used to answer the first research question. Since the model optimizes the total profit, it enables the possibility to reallocate resources. These reallocations are used to answer the second research question.

The reason behind three different case farms is to be able to compare them individually against a reference as well as each other. This in order to evaluate how the answer of the research questions, change with respect to the price of HP-pulp and liquid stillage. This way the generalizability of the study is enhanced. The solution is finally verified against pre-designed feed rations by Rolf Spörndly (Appendix 1) before the results is used.

4.5 Validity and reliability of the study

Validation is about confirmation of how well a model reflects what it is intended to reflect, often the reality. This becomes extra important when a study aims to generate material useful in the real world (Pidd, 2009). Validation in the meaning of a correct reflection of the reality is not possible (ibid). Validation can instead be regarded as a degree of accuracy in chosen methodology. The purpose of validation is that object of intended measurement is the object actually being measured. The study uses persons with insight in the subject to validate that the model performs in a satisfactory manner.

To ensure reliability, the results of the model are compared to actual data from the real world. Further, the study employs an expert in the area of animal nutrition, Rolf Spörndly, to calculate reference feed rations. Reliability is also enhanced via utilization of a sensitivity analysis. A scrutiny of the sensitivity analysis report has the potential to reveal mistakes in data gathering or in the empirical work (Pidd, 2009). The measurement of reliability deals with the dependability of chosen measurement tool and its trustworthiness in produced results. However the restrictions and price levels are strongly connected to the empirical data gathered in the literature review. The model is also built on a series of assumptions that are affected by the authors.

4.6 Ethical issues

Ethical considerations and awareness is important in research (Robson, 2011). There are several aspects to consider from an ethical point of view. A vital part is the referencing process to other people providing information. The description of the informant matters, since the reader interprets and puts values into the description. For instance, participant implies that the person is working in conjunction with the researcher while subject implies that something is done to them (Oliver, 2010). In this section the person who provides information is denoted informant.

It is of importance that all information presented in the thesis is authentic to the original data submitted by the informant. If not so, not only the reliability is at stake, the trust between informant and researcher may be severely damaged (Oliver, 2010). Even simple misunderstandings may cause harm to the informant and be a source error in the validity perspective. It is good to ensure that the interpretation of the received information is accurate by double-check with the informant. Another way to avoid misunderstandings is to be as open as possible and inform about the objective of the study and if there are other stakeholders involved (ibid). It is important to offer anonymity to participants or ask if they may be referred to as a source.

A question worth consideration is if the informant may have incentives to give an inaccurate answer (Oliver, 2010). If so the reliability of the information may take damage. In the context of interpretation and presentation of data, it is important to make a fair presentation without disguise or stress results in an improper way. The researcher also has a role of importance in the case of manage information and sources in a proper way to avoid plagiarism (ibid). The ambition of the thesis is to present the data and findings in a true and fair way and to stress the possibility to alternative interpretations of the results.

5 Empirical setting

The first five sections of this chapter describe important parameters of the model and where they originate. These sections also display the basic assumptions and sources of the underlying facts that form the constraints in the model. The final section displays the empirical model with associated objective function and constraints.

5.1 General settings

The region in focus for the study is the production area of the forest districts of Götaland (Gsk) due to good competitive conditions in this production area. The forest districts of Götaland contain 33 percentages of the dairy cows in Sweden (internet, SJV, 1, 2015). Three more specific locations have been selected to determine the profitability of HP-pulp and liquid stillage. The competitiveness of these two residual based feeds is highly correlated to the distance to the production facilities due to high transportation cost, which is reflected in the pricing of the feed by-products. The locations for the fictive case farms are Osby, Alvesta and Vetlanda (figure. 4).



Figure 4. A map over the southern part of Sweden including the locations of the fictive farms (own modification).

The focus of the study is the profitability of the residuals HP-pulp, produced at Nordic Sugar's facility at Örtofta and Liquid stillage produced at The Absolute Company in Nöbbelöv. The model is developed for a modern dairy barn with 300 cows in the herd to reflect a cutting edge farm. Most of the Swedish cows are held in stables for between 200 and 499 cows (internet, SJV, 2, 2015). The number of cows is fixed in the model due to the nature of the research questions. The case farm has 300 hectares tillable land, of which 50 hectares

of natural pasture is needed to fulfill grazing requirements of the Swedish Board of Agriculture. The requirements are that the intensity of grazing shall not exceed six cows per hectare of pasture (internet, SJV, 3, 2015).

The mature body weight for a Swedish Holstein heifer ready to calve is set to 640 in the model (Volden, 2011:28) and a growth rate of 250 grams per day is used (Spörndly, 2003:14). The bodyweight of a full-grown Holstein cow is slightly above 700 kilograms. The culling rate is 37% out of the dairy life stock (Gunnarsson, 2002).

The duration of one lactation cycle is assumed to be twelve months, which means that the cow calves once a year and the duration of the actual lactation is ten months. The milk produced is measured in energy corrected milk, ECM with a fat content of 4 percentage and a protein content of 3,4 percentage.

5.2 Contribution value

The contribution values are the c_j -value correlating to each action x_j . Region-specific capital budgeting sheets from Agriwise (internet, Agriwise, 1, 2015) are used in the model to estimate contribution values of farm level operations. Agriwise is a well-known economic evaluation and planning tool, developed in collaboration between the Swedish University of Agriculture Sciences and other actors within the agribusiness. It combines science, data from the real world, and is a useful tool with up to date work sheets incorporating current statistics (internet, Agriwise, 2, 2015).

The cost structure of the farm level enterprises is calculated in the model, based upon Agriwise for the Gsk-region. The production cost of crops includes maintenance, depreciation, labor and capital cost (internet, Agriwise, 1, 2015). Important to notice is that the model does not have full cost recovery. The costs that are of low importance, in the context of developing a model that enables the answering of the research questions, is removed (see delimitations). Hence, the profits are measured in modified total profit but in this thesis, the modified total profit is referred to as the total profit.

The model uses the old EU subsidy system as of 2014, due to the current uncertainty in the regulations of the new common agricultural policy. These subsidies have a positive impact on the contribution value, especially for natural pasture.

The price level for input factors is measured during the year of 2014. The discount rate in production calculations for working capital is set to seven percentage which may seem high in relation to the present market situation, but the current low interest rates represents a temporary financial situation that may change quickly. Costs for salaries and social fees associated to work are set to the collective agreement 2013/14 and equals 210 SEK/hour (internet, Agriwise, 1, 2015).

The yield of the crops does not represent an average value for the region. It is an estimate of what should be reasonable to achieve given an effective production. The yields are presented in table 2 specified in kilogram dry matter. The yield level used is after field, storage and preservation losses in the cases where such losses are significant. The production cost includes labor, depreciation, capital cost.

Table 2. The yield levels and production prices of farm produced feed (own modification of internet, Agriwise, 1, 2015).

Feed produced		unit	Wheat	Barley	Oats	Field bean	Maize	Forage	Natural pasture
Yield		Kg DM/ha	6 020	3 956	3 784	3 096	7 800	7 000	1 850
Dry matter		%	0,86	0,86	0,86	0,86	0,22	0,35	0,25
Production price		SEK/kg DM	1,24	1,34	1,35	1,47	2,14	1,68	-0,51

The market price (table 3) is used both to buy and sell crops in the optimization to avoid arbitrage opportunities that may lead to misleading results.

Table 3. Market prices of feeds that the farmers may buy (own modification of Gustafsson et al., 2014; internet, Lantmännen, 2015; internet, SJV, 4, 2015).

Feed bought		unit	Wheat	Barley	Oats	Soya flour	Rapeseed cake	Agrodrank 90	Unik52
Dry matter		%	0,86	0,86	0,86	0,87	0,9	0,9	0,89
Market price		SEK/kg DM	1,70	1,36	1,32	3,85	2,72	2,72	3,99

The price systems of the by-products are based on distance to the plant where the production takes place. This due to the high transportation costs (and low production cost) of the by-products. The prices used in the model are the prices presented in table 4 which are derived from pricelists provided by the delivering companies (Appendix 2).

Table 4. The prices for the by-products HP-pulp and liquid stillage together with the distance between corresponding production plant and the farms (own modification of Appendix 2).

Farm	Örtofta	HP-pulp	Nöbbelöv	Liquid stillage
	Distance (km)	Price (SEK/kg DM)	Distance (km)	Price (SEK/kg DM)
Osby	95	1,50	53	1,16
Alvesta	169	1,70	124	1,68
Vetlanda	251	1,90	200	2,20

Arla is by far the largest dairy cooperative in Sweden (SJV, 2012) and operates in the Gsk-region. Hence the study uses the milk-pricing model of Arla (internet, Arla, 2, 2015) to evaluate the profitability of different feed strategies. Milk price is set to 3,07 SEK based on the price plan of Arla, 19/5-2015. The milk price (P_y) has no specific impact on the answers to the research questions, but it does affect the overall level of profitability, see equation (8).

5.3 Nutritional requirements

Planning a feed ration for milk cows is complex and many factors are necessary to take into consideration. After calving, the cow reaches the maximum production level in the first month and thereafter the production level begins to decline (McDonald et al., 2011). In theory it is possible for the cow to reach a higher maximum production level if the quantity of feed is increased (ibid). However the marginal effect of one kilogram of feed provided to the cow decreases when production level increases due to diminishing returns of feed, see chapter 3. In the model, three production levels are used in order to determine how the marginal effect of feed influences optimal choice of feed ration design and contribute to answering of the research questions.

The nutritional requirements change over time during the lactation period (McDonald et al., 2011). Furthermore the composition of the milk changes depending on time from calving. The model uses ECM to compensate for any composition changes. Substantial changes in feed ration are desirable to avoid, since cows are sensitive to changes in the feed ration. A change in feed ration is more likely to occur when the farmer uses many feed products in the diet. This leads to a more vulnerable position for the farmer if food suppliers have problem with distribution.

5.3.1 Roughage

Since dairy cows are ruminants they have a certain need for sufficient proportion of roughage in the feed mix (McDonald et al., 2011). It can be problematic if the level of roughage is allowed to decrease below a certain point. For example, health disorders may occur when there is a shortage of roughage. Current recommendations are at least a proportion of 35 percentage units of roughage of the total dry matter intake for a dairy cow with a fair production level (Spörndly, 2003:84). However to allow higher milk yields it might not be possible to maintain the recommended proportion. In such a situation 30 % is acceptable. The model applies 35 percentage units as the lowest acceptable proportion of roughage.

5.3.2 Dry matter

The dry matter ration is a key feature to enable measuring nutritional content in feed (McDonald et al., 2011). The dry matter ration is imperative to make different feeds comparable across the same unit of measure. Another reason is that the remaining content is viewed as water, which does not contribute to fulfill the cow's need for nutrients. Hence content of feed in this study is based upon a kilogram of dry matter. The daily feed ration is physically limited to a certain level of dry matter the cow is able to consume. The amount of dry matter a cow can eat is given by function (25) (Bertilsson & Burstedt, 1983:197):

$$DM_{day} = 4,9 + 0,015 \times BW_{lp} + 0,2 \times EM_{lp} \quad (25)$$

BW_{lp} = Average body weight, lactation l , period p .

EM_{lp} = Estimated daily milk yield, lactation l , period p

5.3.3 Energy

In the feed planning process several different measures of energy are used (McDonald et al., 2011). The two most important is metabolizable energy and net energy. *Metabolizable energy*

denotes the amount of energy the cows are able to assimilate. Energy losses occur due to physiological processes in the animal. For example feces, urine and gas emissions, all contain energy. *Net energy* is the total remaining energy that is available for utilization in desirable processes. Energy supplied are used in four main areas; milk production, maintenance, growth, fetal development. The study uses metabolizable energy. The daily energy need is given by function (26) (Spörndly, 2003:14):

$$Energy_{day} = 1,11(0,507BW_{lp}^{0,75} + EM_{lp} \times 5 + G_{lp}) - 13,6 + FD_{lp} \quad (26)$$

BW_{lp} = Average body weight, lactation l , period p

EM_{lp} = Estimated daily milk yield, lactation l , period p

G_{lp} = Energy need for growth, lactation l , period p

FD_{lp} = Energy need for fetal development, lactation l , period p

Energy need for fetal development (table 5) is related to the number of months left to calving which depends on the period, p , and weight which depends on the lactation, l .

Table 5. Energy need for fetal development in mega joules (Spörndly, 2003:14).

FD _{lp} MJ/day		Period		
		p=10	p=11	p=12
Body weight	400	5	8	15
	500	7	11	19
	600	8	13	23
	700	9	15	27

5.3.4 AAT

The second most valuable content in feed is protein. Proteins are used as building blocks in the cow and are essential to enable the milk production. Just like the case of energy, the determinants of required amount of protein are the four main process areas taking place in the cow. Unit of measurement of protein is amino acids absorbed in the small intestine (AAT). The reason is that chosen unit should reflect the amount of protein that the cow is able to utilize (Lärn-Nilsson, 2007). The daily need of AAT is given by function (27) (Spörndly, 2003:14):

$$AAT_{day} = (1,11(0,507BW_{lp}^{0,75} + EM_{lp} \times 5 + G_{lp}) - 13,6) * 7,6 + FD_{lp} \quad (27)$$

BW_{lp} = Average body weight, lactation l , period p

EM_{lp} = Estimated milk yield, lactation l , period p

G_{lp} = Energy need for growth, lactation l , period p

FD_{lp} = Additional AAT for fetal development, lactation l , period p

Additional AAT for fetal development (table 6) is related to the number of months left to calving which depends on the period p and weight which depends on the lactation l .

Table 6. Additional AAT for fetal development in gram (Spörndly, 2003:14).

FD _{ip} AAT/day		Period		
		p=10	p=11	p=12
Body weight	400	41	68	116
	500	51	85	146
	600	59	98	168
	700	66	109	188

5.3.5 PBV

Another important measure of feed to ensure a good feed ration with satisfactory protein supply is the balance of protein in the rumen (PBV). The process of protein synthesis in a cow mainly takes place in the rumen (Lärn-Nilsson, 2007). Microbes perform the synthesis and they use degraded protein, ammonia as building stones. To enable the synthesis of protein it is important that the levels of ammonia in the rumen are sufficiently high and do not fluctuate significantly. The other aspect of PBV is that the level of energy in the rumen is satisfactory to support an adequate pace of microbe growth (ibid). If there is a shortage in energy the amount of microbes is too low to absorb all the degraded amino acids. Thus an unbalanced level of energy in relation to nitrogen leads to insufficient utilization of the feed. This leads to feed efficiency losses that have a negative effect on the profitability of the feed rations. When PBV of a feed ration is positive, it is an expression for excess of nitrogen in the rumen (Magnusson et al., 1990). The optimal rate of PBV in a feed ration is zero. Recommended interval, used in the model, is 0-300 (Spörndly, 2003:14).

5.3.6 Starch

Starch content in the feed ration is essential for the functionality of the rumen (Volden, 2011). Too high levels of starch in the feed ration may have negative effects on the roughage utilization and reduce the fiber digestibility. The starch content in the feed ratio should not exceed 25 percentage units of the total amount of dry matter. Insufficient starch level may lower the microbial activity in the rumen and lead to negative effects on protein synthesis.

5.3.7 Crude fat

According to feed recommendations, content of crude fat in a feed ration should be at a level of maximum five percentages of total dry matter intake (Wiktorsson, 1988). At higher levels of fat content the cow's digestion of fiber is inhibited. The reason is that high levels of fat in the rumen can have a constraining or even a toxic impact on the microbes. In the model, crude fat may not exceed five percentage units of the calculated dry matter.

5.3.8 NDF

A restriction of feed composition similar to the roughage condition is NDF, neutral detergent fiber. Maximum feed consumption of NDF is recommended to 1,5 percentage units of live body weight (Nycander, 1989). Recommended minimum proportion of NDF in the feed ration is 28 % (NRC, 1988). These levels represent the maximum intake a cow can consume in a day and the minimum level to satisfy their appetite.

5.4 Nutritional content of feeds

The data about nutritional content in different feed (table 7) is primarily gathered from feed tables at the Department of animal nutrition and management at SLU, (internet, SLU, 2015). However some data is collected from the organization Växa Sverige (internet, Växa Sverige, 2015) when data is not available at SLU:s feed table.

There is a level of uncertainty in the nutritional values mainly of forage due to annual variations. Out of the factors that may be controlled by the farmer, choice of strategies for seeding, fertilization and harvest have the most impact on the nutritional values of forage (pers. Comm., Aurell-Svensson, A., 2015). The variety choice of ley does not have the same effect on the nutritional value of the feed (ibid). Therefore the model uses one, in the region common, variety of ley. Energy and protein content increases with the number of annual harvests (Frankow-Lindberg, 2013). In the Gsk-region, it is common with two to three lay harvests per year (pers. Comm., Aurell-Svensson, A., 2015). The model reveal that the intense three harvests system almost always is preferred over the more extensive system with two harvests due to lower production cost per kg produced feed. Therefore the extensive forage system is excluded from the final model in order to avoid unnecessary complexity.

Table 7. The nutritional content of feed used in the model (own modification of internet, SLU, 2015; internet, Växa Sverige, 2015).

	Field bean	Maize	Natural forage	Winter pasture	Winter wheat	Barley	Oats	HP-pulp	Soya flour	Rapeseed cake	Liquid Stillage	Agrodrank 90	Unik52	
Feed content														
Dry matter (%)	86%	22%	35%	25%	86%	86%	86%	27%	87%	90%	90%	8%	90%	89%
Energy (MJ)	13	11,4	10,1	9,4	14,1	13,2	11,7	12,8	14,6	12,4	15,8	13,6	13,3	14
AAT (g)	96	80,8	69	72	95	90	67	100	182	220	89	120	116	157
PBV (g)	133	-70	14	-26	-33	-29	-2	-69	261	79	173	185	142	80
Starch (g)	366	348	85,5	0	644	518	338	5	62	9	10	50	0	38
Crude fat (g)	19	22	20	20	25	27	61	8	10	46	177	68	45	96
NDF (g)	190	355	569	612	138	229	358	445	95	332	242	400	270	297

5.5 Milk production

The optimization uses the same yield function of ECM production as Norfor. The advantage with the yield function of Norfor is the breed specific elements in the function. The lactation curve is given by function (28) (Volden, 2011:28):

$$EM = a + b * Yherd - c * DIM + \ln(DIM) * d \quad (28)$$

EM is the estimated milk yield in kg ECM per day, Yherd is the annual yield per cow for the herd in focus based on 305 days in lactation, DIM is the number of days in lactation and finally a, b, c and d are breed specific regression coefficients (table 8) (Volden, 2011:28).

Table 8. Regression coefficients of the lactation curve function, valid for the Swedish Holstein (Volden, 2011:28).

Regression coefficients Swedish Holstein				
	a	b	c	d
Primiparous (PP)	-4,05	0,00299	0,0356	2,591
Multiparous (MP)	2,93	0,00299	0,061	1,997

The actual average yield 2014 for Swedish Holstein (Kokontrollen, 2015) is used to validate the chosen production level. Figure 5 below shows the daily average production levels month one to ten in the lactation period. The red piles show the average actual yield level for a Swedish Holstein in year 2014 as a reference level and the blue piles display the estimated yield level calculated by the yield function (28). The figure shows booth primiparous (cows in first lactation), which are the two left piles in each formation of four piles. The two right piles in each formation represent Multiparous.

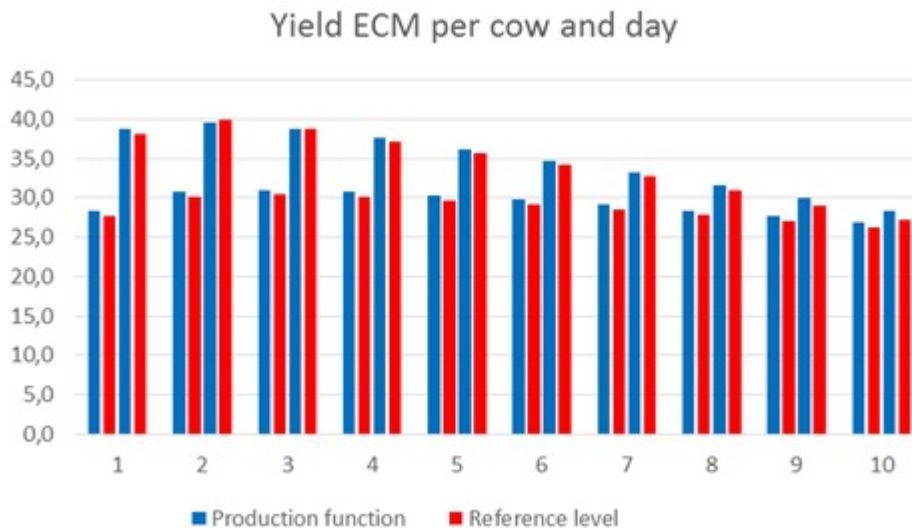


Figure 5. The production level of milk in period 1-10 as an outcome of the production function (blue), as well as the real farm levels (red). The left two piles of each formation represents primiparous and the right two represents multiparous (own modification of Kokontrollen, 2015).

5.6 Empirical model

This section contains a detailed overview of the optimization model used in the study. The constraints are based on the nutritional requirements of dairy cows, presented in section 5.3.

5.6.1 Objective function

The objective function designed for use in the model is an extension of the profit maximizing function, equation (8), developed in the theoretical framework. The objective function formulated in equation (29) provides a more detailed production function and is specified for specific crops and feed applicable to this study. The study identifies two dimensions with

major impact on the lactation curve, which determines the shape of the production function for milk. These are lactation number and a time perspective that is divided on a monthly basis. Cows can remain in production for several years. Yet the study only distinguish between first and following lactations in order to keep the empirical programming in a comprehensible extent. Furthermore the main categories of feed are specified for eligible options.

$$\begin{aligned} \max \pi = & P_y \sum_{l=1}^2 \sum_{p=1}^{12} [f_{l,p}(X_k, X_g, X_a)N] + \sum_{k=1}^3 [P_k(A_k Y_k - N X_k) - C_k A_k] - \sum_{g=1}^4 [C_g A_g] \\ & - \sum_{a=1}^7 [P_a N X_a] - FC \end{aligned} \quad (29)$$

N	=Number of cows in production
P_y	=Milk price
$f_{l,p}(X_k, X_g, X_a)$	=Production function for milk production, variables three categories of feed. Two dimensions of lactation and period also determine the function.
l	=Lactation number
p	=Period in lactation stage
X_k	=Kg DM of feed grain per cow
X_g	=Kg DM of forage or silage per cow
X_a	=Kg DM of alternative feed products per cow
k	=Feed that can be bought and grown
P_k	=Price of feed grain per Kg DM
A_k	=Land for grain production
Y_k	=Yield of grain production, kg DM per ha
C_k	=Variable cost for grain production
g	=Feed that only can be grown
C_g	=Variable cost for farm based feed
A_g	=Land for feed production
a	=Feed that only can be bought
P_a	=Price of purchased feed per Kg DM
FC	=Total fixed costs
α_g	=Maximum share of forage or silage of total land
α_k	=Maximum share of grain of total land
e_k	=Nutritional supply of grain per Kg DM
e_g	=Nutritional supply of forage or silage per Kg DM
e_a	=Nutritional supply of purchased feed per Kg DM
$E_{DM}(l, p)$	=Nutritional requirement of dry matter depend on lactation and period
$E_R(l, p)$	= Nutritional requirement of roughage depend on lactation and period
$E_E(l, p)$	=Nutritional requirement of energy depend on lactation and period
$E_{AAT}(l, p)$	=Nutritional requirement of AAT dependent on lactation and period
$E_{PBV}(l, p)$	=Nutritional requirement of PBV depend on lactation and period
$E_S(l, p)$	=Nutritional requirement of starch depend on lactation and period

$E_{CF}(l, p)$	=Nutritional requirement of crude fat depend on lactation and period
$E_{NDF}(l, p)$	=Nutritional requirement of NDF depend on lactation and period
$BW(l, p)$	=Body weight as a function of lactation and period

5.6.2 Constraints

The framework presented alongside equation (8) includes aspects regarding the main constraints for the profit maximization problem of a dairy farmer. These key constraints are described in detail and new aspects are introduced. For the interested reader is an overview of the constraints associated to the model presented in appendix 3.

Crop production

Max *land*
The fictional farms each operate a certain amount of tillable land. This is illustrated in equation (30). Land is engaged in crop production operations at the farm. The farmer cannot exceed the maximum amount of available land. \bar{A} represents the maximum available land the farmer has to allocate to different crops. A_k denotes the arable land used for production of grain crops. A_g refers to the share of total land used for forage and silage production. The variety of crops the farmer is able to grow represents a typical dairy farm. The possible choices are, wheat, barley, oats, field beans, maize, forage and natural pasture.

$$\sum_{k=1}^3 A_k + \sum_{g=1}^4 A_g \leq \bar{A} \quad (30)$$

Crop rotation

The farms have a crop rotation to prevent complications in the crop production. The crop rotation is illustrated in equation (31) and is designed on a eight-year basis, with some room for adaption. The crop rotation applies regardless of the purpose of the crops, (feed or marketable crop). In table 9, the maximum shares, $\alpha_{k,g}$, that the crop rotation allows are displayed.

$$A_{k,g} \leq \bar{A} \alpha_{k,g} \quad (31)$$

Table 9. Maximum allowed shares of each crop according to the crop rotation (own illustration).

Crop	$\alpha_{k,g}$, Max share of total land
Winter wheat	3/8
Spring barley	2/8
Oats	2/8
Field bean	1/8
Maize	1/8
Forage	1 hectare \leq 0,33 ha spring grain
Natural pasture	Max 6 cows per hectare

Feed ration design

Dry

matter

A cow is not able to consume more feed than its stomachs can accommodate. The amount a cow is able to consume is restrained by equation (32). The left hand side of the equation expresses supplied DM. The content of DM in each feed in relation to the amount of each feed equals the supplied amount. Accordingly, the maximum quantity of dry matter is represented by the right hand side. The maximum quantity is a function of age and time from calving.

$$\sum_{k=1}^3 e_k X_k + \sum_{g=1}^4 e_g X_g + \sum_{a=1}^7 e_a X_a \leq \sum_{l=1}^2 \sum_{p=1}^{12} E_{DM}(l, p) \quad (32)$$

Roughage

Since cows are ruminants they need a certain share of roughage in the feed ration. Equation (33) ensures that this restriction is met. The required amount is given by the right hand side of the equation. Required amount depends on how much milk each cow produces, which is determined by lactation number and time from calving.

$$\sum_{k=1}^3 e_k X_k + \sum_{g=1}^4 e_g X_g + \sum_{a=1}^7 e_a X_a \geq \sum_{l=1}^2 \sum_{p=1}^{12} E_R(l, p) \quad (33)$$

Energy

One of the key elements for milk production is energy supply. Energy supply is not allowed to be less than the energy demanded and the relationship is illustrated in equation (34). Energy demand is directly related to the position on the lactation curve.

$$\sum_{k=1}^3 e_k X_k + \sum_{g=1}^4 e_g X_g + \sum_{a=1}^7 e_a X_a \geq \sum_{l=1}^2 \sum_{p=1}^{12} E_E(l, p) \quad (34)$$

AAT

Another key component of milk production is AAT, amino acids absorbed in the small intestine. The nutritional constraint of AAT is expressed by equation (35). Similarly to the case of energy, the supplied quantity of AAT is not allowed below a certain level. The required quantity of AAT also depends on the lactation curve.

$$\sum_{k=1}^3 e_k X_k + \sum_{g=1}^4 e_g X_g + \sum_{a=1}^7 e_a X_a \geq \sum_{l=1}^2 \sum_{p=1}^{12} E_{AAT}(l, p) \quad (35)$$

PBV

PBV, protein balance in the rumen, is introduced in the process of feed ration design in order to maintain a profitable ratio between energy and protein content. Consequently, the PBV-value of the feed ration has to be defined into a tight interval to avoid inefficient feeding strategies. However, it cannot be too limited. In that case the flexibility in feed ration design would be

discouraged. The PBV-constraint that is formulated for this study is illustrated in equation (36). The middle part constitute the PBV-value of the feed ration. The left and right hand sides establish the allowed interval.

$$E_{PBV_{min}} \leq \sum_{k=1}^3 e_k X_k + \sum_{g=1}^4 e_g X_g + \sum_{a=1}^7 e_a X_a \leq E_{PBV_{max}} \quad (36)$$

Starch

Content of starch in the feed may disrupt the digestive system of the cow. In order to prevent possible production losses the share of starch has to be restrained. The starch-constraint is presented in equation (37). The amount of starch supplied is not allowed to increase above a certain level. The maximum allowed quantity is correlated to the production level of milk.

$$\sum_{k=1}^3 e_k X_k + \sum_{g=1}^4 e_g X_g + \sum_{a=1}^7 e_a X_a \leq \sum_{l=1}^L \sum_{p=1}^P E_S(l, p) \quad (37)$$

Crude

fat

Similar to the case of starch crude fat may have a disruptive effect the upon the digestive system of the cow. The amount of crude fat content also has to be restrained. The crude fat content of the feed ration is constrained by the relationship expressed in equation (38). The maximum allowed crude fat content is expressed by the right hand side of the equation. The maximum level is determined by the orientation of the lactation curve.

$$\sum_{k=1}^3 e_k X_k + \sum_{g=1}^4 e_g X_g + \sum_{a=1}^7 e_a X_a \leq \sum_{l=1}^L \sum_{p=1}^P E_{CF}(l, p) \quad (38)$$

NDF

NDF, neutral detergent fiber, is a relatively new concept within feed ration design. It has a similar effect for feed ration composition as the roughage constraint. The constraint represented by equation (39) is developed to meet the NDF-criterias. The middle part of the equation represents supply of NDF. A low fiber content has troublesome affects on the digestive system of the cow since ruminants require a sufficient share of fiber feeds in the feed ration. However, if the share of fiber is too high it also has a negative aspect. The cow would not be able to consume sufficient feed volumes if NDF is allowed to reach levels exceeding recommended quantities. The reason is that feeds with high fiber content require more space in the digestive system and the digestion pace is slower.

$$\sum_{l=1}^L \sum_{p=1}^P E_{NDF}(l, p) \leq \sum_{k=1}^3 e_k X_k + \sum_{g=1}^4 e_g X_g + \sum_{a=1}^7 e_a X_a \leq \sum_{l=1}^L \sum_{p=1}^P 0,015 BW(l, p) \quad (39)$$

6 Results

In this chapter the main results of the model are presented. These results are of major interest to be able to answer the research questions. The complementary results are presented in Appendix 4 for the interested reader.

6.1 Profitability of case farms

Modified total profits of each case farm evaluated in the study are illustrated in figure 6 below. Total profit of all farm operations incorporates the two production systems of the farms, dairy production and crop production. The total profit of the reference farm is 5 890 KSEK (thousand Swedish crowns). Total profit of the farm located in Osby is 6 629 KSEK. This is an increased profit in the case of Osby with 739 KSEK, which is an increase of 12,6 % compared to the reference farm.

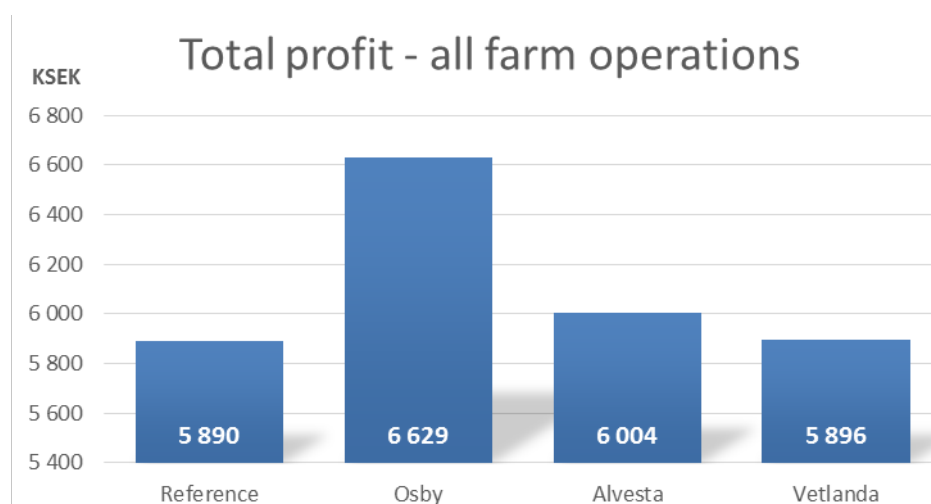


Figure 6. The total profit of all farm operations at the case farms (own illustration).

The farm in Alvesta increases total profits to a level of 6 004 KSEK if the farm utilizes the opportunity to use by-products as feed. The profit of the Alvesta farm is 114 KSEK higher than the reference farm. The farm located in Alvesta increases its profit with 1,9 % compared to the profit level of the reference farm. The Vetlanda farm exhibits a slightly increased total profit at a level of 5 896 KSEK. The increase amounts to 6 KSEK compared to the reference. The profit of the Vetlanda farm experiences a moderate increase of 0,1 % in comparison with the reference profit level.

The different levels of the IOFC per Kg produced milk are presented in figure 7. Income over feed cost of the reference farm sums up to 1,87 SEK per kilogram of ECM. The IOFC amounts to 2,10 SEK/Kg ECM in the case of the farm located in Osby. The difference between the two farms amounts to 0,23 SEK/Kg ECM in benefit for Osby. This implies that the Osby farm earns 0,23 SEK more per kilogram milk produced than the reference farm. Thus the feed ration employed by the Osby farm is 12,6 % more efficient in terms of profitability.

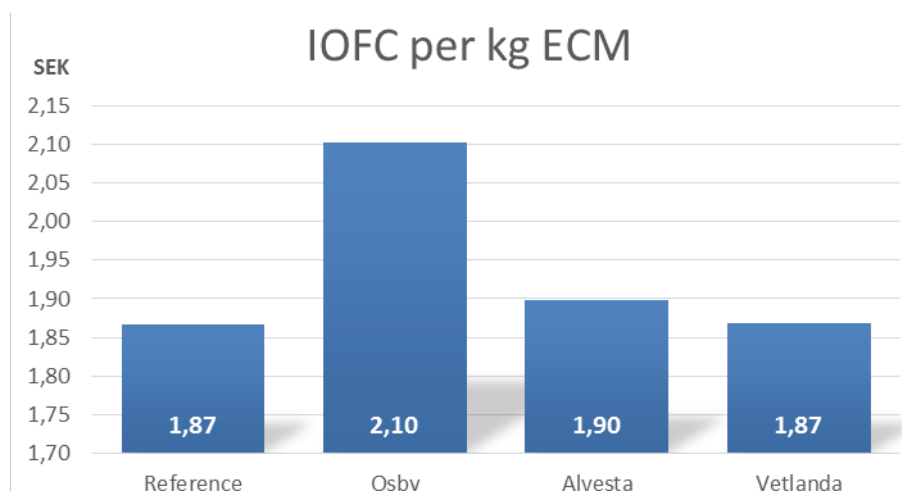


Figure 7. The income over feed cost of the case farms (own illustration).

The Alvesta farm exhibits an IOFC at a level of 1,90 SEK/Kg ECM. Alvesta hence earns 0,03 SEK/Kg ECM more than the reference. The efficiency of the feed ration engaged by Alvesta is 1,7 % higher than the feed ration of the reference farm. The farm in Vetlanda displays an IOFC at a level of 1,87 SEK/Kg ECM. The level of the IOFC at Vetlanda is almost equal to the level of the reference farm, 0,001 SEK/kg ECM higher. Thus the feed ration employed by the Vetlanda farm is 0,05 % more efficient than the one utilized by the reference farm. Although the efficiencies of the two feed rations of the reference and the Vetlanda farm are similar the feed rations are still different in composition.

It is important to note that the changes in total profit and the changes in IOFC per Kg ECM in the comparison above expressed in percentages, are not equal. This observation is important to bear in mind in order to comprehend the analysis later in the thesis.

Another dimension of feed ration competitiveness are indirectly visible in figure 7, for example the feed costs of each farm. Remember that the milk price employed in the empirical study is fixed to a level of 3,07 SEK/Kg ECM. Thus the feed cost on the reference farm amounts to 1,20 SEK/Kg ECM. The farm located in Osby exhibits a feed cost of 0,97 SEK/Kg ECM. Alvesta has a feed cost of 1,17 SEK per produced kilogram of ECM. In the case of Vetlanda the feed cost is 1,20 SEK/Kg ECM. Two farms with identical IOFC per kilogram of produced ECM display identical costs for producing a kilogram of ECM, given that they reach the same production level.

6.2 Resource allocation

Land allocation at each case farm is displayed in table 10. Given the presence of dairy production the study identifies four major crops that claim the available land: natural pasture, forage, barley and winter wheat. Wheat is the only crop exclusively grown as a marketable commodity. The remaining three crops are solely grown for feed purpose.

Natural pasture is observed to be the only crop presented in table 10 that has a fixed share of available land with no apparent correlation to the amount of employed by-products. All farms grow 50 hectare of natural pasture. The allocation of the remaining 250 hectares differs

between the case farms as purchased quantities of by-product feeds vary. The reference farm engages 101 hectare in wheat production. The Osby farm increases wheat production with 11,7 %. The farm located in Alvesta displays an increased wheat production of 7,0 % compared to the reference farm. Even the farm in Alvesta increases wheat production marginally, to an extent of 1,2 %. Note, that land allocation differences have implications for the distribution of revenues generated from the two production systems.

Table 10. Crop allocation at case farms (own illustration).

Crop allocation (hectare)				
	Reference	Osby	Alvesta	Vetlanda
Winter wheat	100,7	112,5	107,7	101,9
Barley	37,3	37,0	35,6	37,0
Forage	112,0	100,5	106,7	111,0
Natural pasture	50,0	50,0	50,0	50,0

The two remaining crops are forage and barley, which both are grown for feeding purposes. It is important to note that a correlation exists between these crops. Hence, the lowest allowed acreage allocated to barley and oats depends on the required proportion of forage in the feed ration. More precisely, land allocated for production of barley and oats has to be at least a third of the land reserved for forage production, see chapter 5.

The preferred resource allocation displayed in table 10 also has implications for the shadow price of total land. The chosen resource allocation on the other hand is affected by the forage re-seeding constraint, which also has implications on the opportunity cost of grain production. In the case of the Osby farm the re-seeding constraint for forage is not binding, i.e. λ_1 is equal to zero. The remaining case farms however all suffer from a binding re-seeding constraint. The marginal cost of the binding re-seeding constraint amounts to 2 674 SEK per hectare. This leads to that the Lagrangean multiplier of Osby for total land merely is 58 SEK per hectare at current production level. Meanwhile, all other case farms has a λ_1 of 2 733 SEK at the current state.

Another aspect of altered resource allocation imbedded within the results in table 10 is the fact that feed production requires more work hours than grain production per hectare produced. Thus, the land allocation has impact on labor needs of the farm. The amount of work hours and the differences between the case farms are displayed in Appendix 4.

6.3 Operational cost of forage

A key component in derivation of the feed cost is costs related to the production of forage. The feeds that are produced at farm level have to be priced at the operational cost to capture impacts on all farm operations. The general formula for computing the shadow price of forage is illustrated by equation (20) in chapter 3. $P_g = \frac{c_g + \lambda_1}{y_g} - \lambda_2 e_g$. Operational cost of forage is mainly determined by the opportunity cost of not being able to allocate the land for grain production. Opportunity cost is indirectly visible in equation (20). Opportunity cost is a part

of λ_1 , the shadow price of one additional hectare of land. Shadow price of land is mainly deduced from opportunity cost of grain production, but also to some extent from dairy production. The proportions depend on which commodity is more profitable to produce. The right hand side of equation (20) illustrates how shadow price of forage also is dependent on the nutritional content in forage, e_g , and the marginal cost of the roughage constraint in the process of feed ration design, λ_2 , see chapter 5.

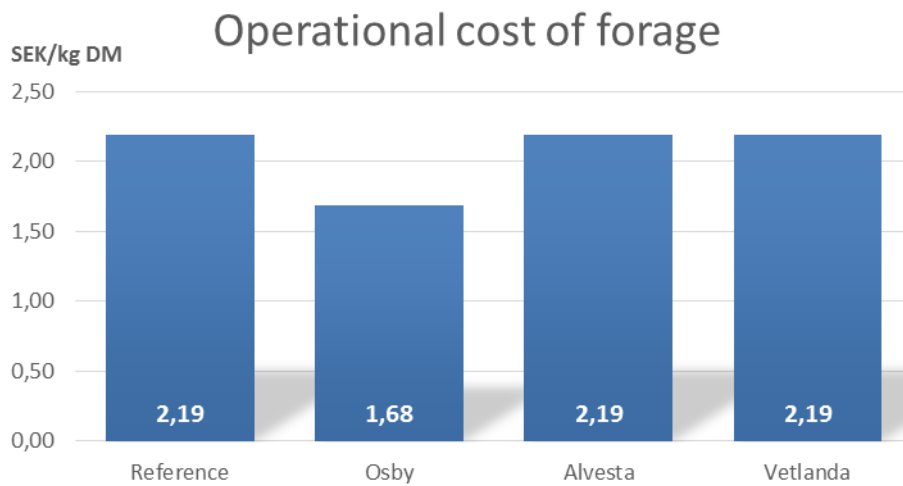


Figure 8. The operational cost of forage production at the case farms (own illustration).

The different operational costs of forage observed in the study are presented in figure 8. At the reference farm the price of forage is 2,19 SEK per kg DM. The price of forage at Osby farm is 1,68 SEK per kg DM. The shadow prices of forage at the Alvesta and Vetlanda farms are equal to the level of the reference farm.

The results displayed in figure 8 also provide information about the forage re-seeding constraint, which not are included in the formula for operational cost of forage above. The re-seeding constraint does however affect the operational cost of forage since it determines the size of the opportunity cost of grain production. The marginal cost for the forage re-seeding is still the same as described above. The pattern illustrated in figure 8 is also indirectly visible in table 10, whereas Osby allocates more land for barley production than is needed for re-seeding of forage.

6.4 Results from the sensitivity analysis

In this section results from the sensitivity analysis are presented. The concept of optimization, which only gives a snapshot of the reality, provides the legitimization of the following results. A sensitivity analysis is the final part of the optimization process that serves as a validation of the result. It also makes the results more reliable and comprehensive since shifting market conditions are a part of the business environment.

The object of these results is to mimic real life possible occurrences that the farm manager can be exposed to. The three events: milk yield changes, grain price changes and crop yield changes, differ in terms of manageability. For example are milk yield more likely to be

influenced by the farmer than the remaining occurrences, which are more correlated to external implications like weather conditions and settings on the world market.

The presentation of the sensitivity analysis results is based the baseline scenario with associated results presented earlier in chapter 6. Then each sensitivity analysis has one increased level and one decreased level of the occurrence in question. The comparison between the difference results is made with regard to the baseline profit.

6.4.1 Changes in milk yield

Figure 9 illustrates the effects of a change in milk production levels and their implications on modified total profit. The Osby farm exhibits the highest level of total profit. At a milk production level of 12 000 Kg ECM the Osby farm has a profit of 7 592 KSEK per year. In opposite, the reference farm has the lowest profit of 4 551 KSEK at the lowest production level.

Figure 9 also reveals information about which farms display the biggest changes in total profit when milk production level changes. The Vetlanda farm has the biggest profit increase when the production level increases to 12 000 Kg ECM. The profit increase equals to 1 298 KSEK per year. The farm located in Osby is the farm that displays the smallest benefit of an increased production level, +963 KSEK. Contrary, it is the Alvesta farm that is the least exposed for a decrease in milk production, -953 KSEK. The farm located in Osby exhibits the largest loss in profits due to decreased milk production. The loss equals to 1 342 KSEK on annual basis.

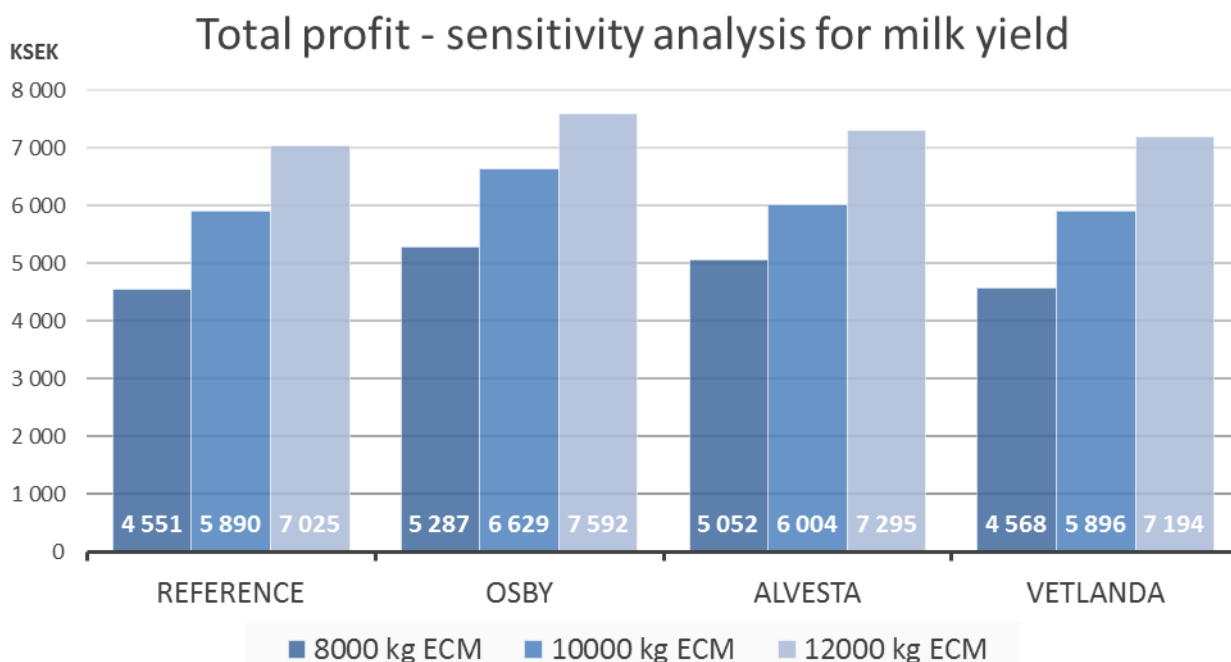


Figure 9. Changes of total profit in relation to milk yield level of the herd (own illustration).

The results displayed in figure 9 also have a direct correlation to IOFC per Kg ECM. Note, that the only initial difference from the baseline results is the milk production level. This on the other hand has implications of the IOFC per Kg ECM since the feed cost is distributed on more or less Kg ECM. Hence IOFC per Kg is altered.

Another dimension of the altered IOFC relates to the rule of diminishing returns presented in chapter 3. The implication is that a higher production level of milk leads to increased feed requirement per produced Kg ECM.

6.4.2 Changes in grain price

Figure 10 presents the effects of a change in grain price levels and their implications for total profit. In this figure there is no clear pattern. The reference and Vetlanda farms display a disadvantage from increased grain prices. In reverse, the farm located in Osby exhibits increased profits as grain prices rise. Then there is the Alvesta farm, which display increased profits from both lower and higher grain prices compared to the baseline price level.

The Osby farm still displays the highest profit and it occurs at the higher price level of grain. The increased profit sums up to 6 771 KSEK per year, which is an increase of 142 KSEK. Also in this occurrence the reference farm exhibits the lowest profit at 5 689 KSEK per year. Which contradictory occur at the higher price level of grain. The lower level of profit at the reference farm represents a decrease of 201 KSEK compared to the baseline scenario.

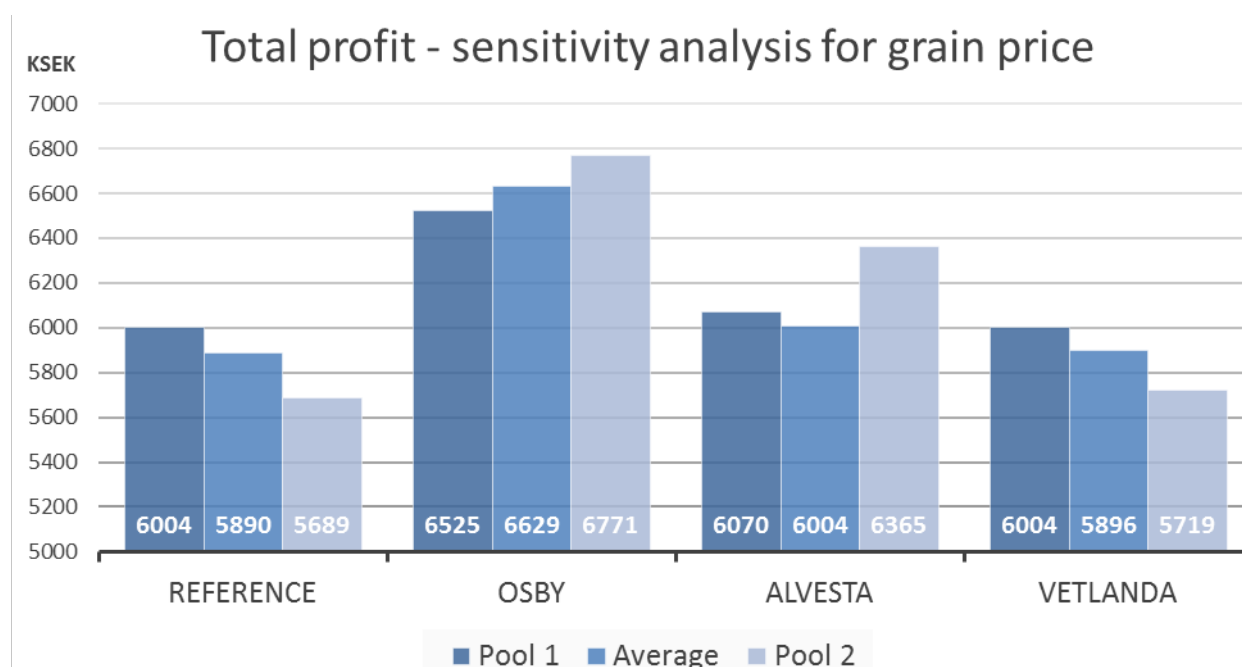


Figure 10. Changes of total profit in relation to the price level of grain (own illustration).

In both figure 9 and figure 10, the reference and Vetlanda farms exhibit similar patterns, as the conditions change and they display approximately equivalent financial results. The similar behavior of the two farms relate to the geographical position of the Vetlanda farm. It is located on the verge of area where the by-products are a competitive feed option. Hence, the small difference between the Reference farm and Vetlanda farm relate to the restrained utilization of by-products in the feed ration at Vetlanda farm.

Changes in grain prices also have implications on deduction of operational cost for farm-produced feed like forage. A higher grain price has effect on the opportunity cost of grain production. An altered operational cost has effect on the competitiveness of the feed products in the feed ration design. Thus, feed ration, IOFC and profit are all altered by changing grain prices.

6.4.3 Changes in crop yield

Figure 11 illustrates the effects of a change in crop production levels and their implications on total profit. Yet again it is the Osby farm that reach the highest profit. At the higher yield level of crop the Osby farm displays a profit of 6 757 KSEK per year. Similarly to earlier occurrences it is the reference farm that exhibits the lowest profit. The reference farm produce a profit of 5 721 KSEK per year at the lowest yield level.

Figure 11 furthermore contain information about the disadvantages and benefits of the farms due to changing yield levels of crops. The reference farm displays the largest profit increase when the highest production level of crop occurs. The profit increases with 550 KSEK per year. The farm in Osby exhibits the smallest profit increase at the highest production level compared to the baseline scenario, +128 KSEK. In opposite, the Vetlanda farm experiences the lowest loss in profit at the lowest production level, -153 KSEK. Also in this occasion, it is the farm located in Osby that suffers the biggest loss in profit. At the lowest production level of crop the Osby farm displays a decreased profit of 510 KSEK per year. The pattern in figure 11 is quite apparent and resembles the one displayed in figure 9.

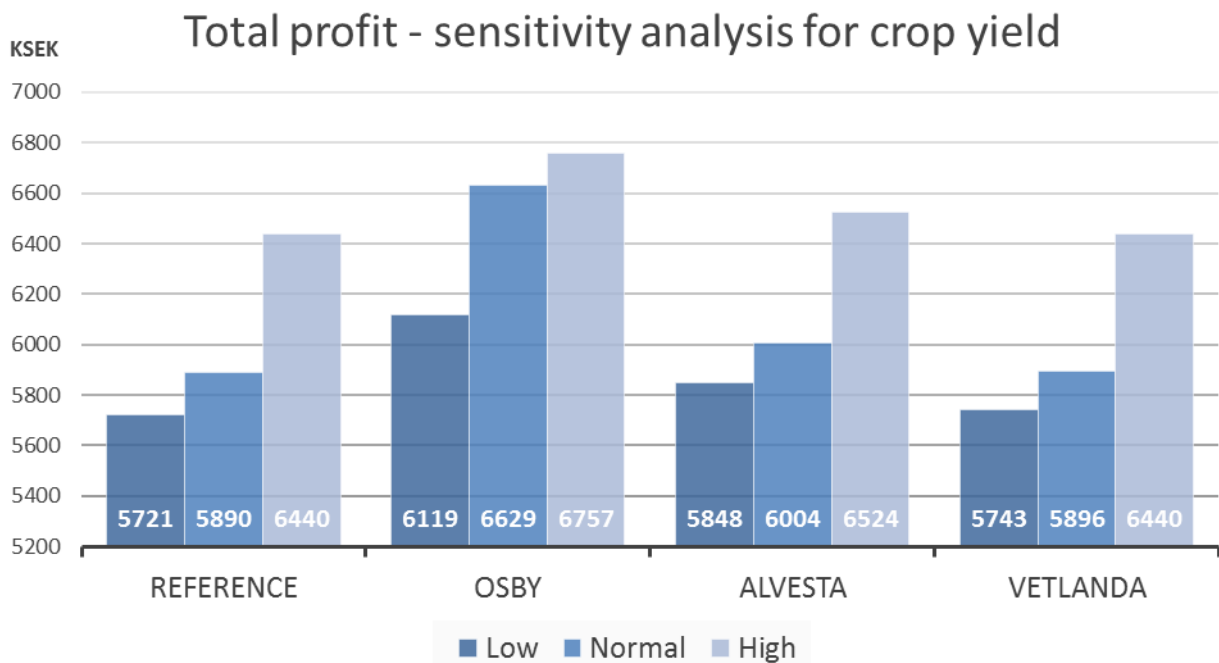


Figure 11. Changes of total profit in relation to yield level of crops (own illustration).

Similar to the case of figure 10, changing yield levels of crops affect the size of operational cost of home grown feeds. The opportunity cost of growing marketable grain increases since grain production becomes more profitable. On the other hand leads a higher yield level of farm-produced feed to an increased quantity, which the increased opportunity cost is distributed on. Hence, it is not clear if the operational cost decreases or increases. It depends on farm specific criterions and the conditions in the baseline scenario of the different farms.

7 Analysis and discussion

In this chapter the empirical results are analyzed based on the theory. The results are then compared to results from prior studies to estimate the reliability and validity of the results in the discussion. The objective is to answer the research questions of the study posed in chapter 1.

The aim of the study is represented by the following research questions:

- How does the opportunity to incorporate by-products in the feed ration affect total profit at farm level?
- How does optimal alternative feed strategies affect the resource allocation at farm level?

7.1 Analysis of main results

The major tendency is a declining total profit and that the competitiveness of by-product feeds decreases as distance to supplying plants increases. All farms that employ by-products in the feed ration obtain a higher IOFC, compared to the reference farm. The observation is supported by the theory of an optimization subjected to restrained optimal behavior via binding constraints in the optimization model (Debertin, 1986).

7.1.1 Profitability implications

Osby

The increased total profit of Osby by 739 KSEK (+12,6 %) originates from shifting profitability margins in both production systems. The increase in IOFC per Kg produced ECM is also 12,6 %, but slightly higher. This indicates that the profitability of dairy production increases more than total profit, since the level of milk production is unaltered. Hence, the profitability of grain has decreased marginally. The observation is also supported by the increase in allocated land for wheat production in the case of Osby, +11,7 %. The relative shifts in land allocation between the farms are smaller for Osby in the case of land allocation compared to shifts in profitability.

The reason behind the negative slope of profitability in crop production for Osby is the law of diminishing returns explained in chapter 3 (Debertin, 1986). As crop production reaches a certain level production the relative profitability of employed inputs decreases. At a certain production level the farmer creates losses if he increases produced amount further. The maximum level of a profitable production amount is given by $VMP = MFC$ (ibid).

Alvesta

The farm located in Alvesta experiences a lower increase in profitability than Osby. The profit is enhanced with 114 KSEK, which corresponds to an increased profit of 1,9 % compared to the reference farm. Also in the case of Alvesta the change in total profit originates in the production of the farm's two commodities. In comparison total farm profit increases with 1,9 %, but IOFC only accounts for an increase of 1,7 %.

The interpretation is that the Alvesta farm has not reached the point for profit maximizing level of crop production (Debertin, 1986). Alvesta has the possibility to expand crop production and still increase profit of grown hectares. The statement is supported by observed change in resource allocation. The farm located in Alvesta increases wheat production with 7 % compared to the reference farm. In comparison with Osby land allocated for wheat production for Alvesta increases more than profitability, +1,9 %. The reason is that Alvesta has more to gain from increased wheat production in comparison to Osby, due to the law of diminishing returns (ibid).

Vetlanda

The farm in Vetlanda displays the lowest profit increase of the farms, except the reference farm. Vetlanda experiences an increase of 6 KSEK on annual basis, which represents a profit increase of 0,1 %. Even if the profit change is moderate the farm experiences a change in profitability of the two production systems and a change in resource allocation. The modest profit increase of 0,1 % is only explained by a 0,05 % increase in IOFC, due to the law of diminishing returns. Hence, the remaining profit increase is generated from altered resource allocation in favor of crop production.

The explanation is similar to the one applying to the case of Alvesta. Vetlanda has the possibility to increase total farm profit through an expanded crop production. The reason is the relative position on the profit maximization curve of the two production systems (Debertin, 1986). The preferred production system is the one where the room for increased production is the biggest, i.e. the production system that is furthest away from the profit maximizing level of production.

The interpretation is supported by preferred land allocation for wheat production. The Vetlanda farm increases wheat production with 1,2 %, still profit is only enhanced by 0,1 %. This implies that the Vetlanda farm in the current state has best possibility of profit increase via expansion of wheat production (Debertin, 1986). However, a situation with cheaper alternative feed products would change the conditions significantly, as shown by the other case farms.

7.1.2 Model implications

The perceived differences in shadow price of total land is as mentioned mainly dependent on if the re-seeding constraint of forage is binding or not, which also has implications on opportunity cost of grain production. A not binding re-seeding constraint of forage leads to a lack of opportunity cost for grain production, since allocation of land for grain production no longer is restrained. The phenomenon is supported by equal differences in operational cost of forage and shadow price of total land.

The reason behind the observed phenomenon is based in the fundamentals of profit maximization (Flaten, 2001). The sizes of λ_1 and P_g is determined by how restrained the optimal behavior is by one or several constraints at the same time as the profitability of each production systems also has a significant affect.

The observed values of λ_1 are 58 SEK for Osby and 2 733 SEK for remaining farms. The main reason behind the significant difference is lack of binding forage re-seeding constraint for Osby. However, another dimension is the law of diminishing returns (Debertin, 1986). Osby has reached a state where crop production is at its peak. Neither is more land for feed

production of major interest since the Osby farm has minimized feed costs through a higher share of purchased feeds, specifically by-products feeds. Chosen resource allocation thus leads to a cost structure that marginally benefits from more land inputs.

Remaining farms on the other hand is prepared to pay more for an expansion of total land. The reason is their restrained optimal behavior due to the forage re-seeding constraint (Flaten, 2001). These farms have a lot to gain from increased total land since they have room for expansion and profitability enhancement in their grain production.

The second Lagrangean multiplier computed in chapter 3 is λ_2 . Which represents all marginal costs associated with the constraints determining the options in the process of feed ration design. Each λ_2 has a value if the constraint is binding for the computed feed ration (Debertin, 1986). Which constraints that are binding are dependent on utilized feed products, since the study has a wide range of optional feed products. The preferred feed products of each farm are in turn determined by faced prices of the different feeds. Grown or purchased feed products have no implication on λ_2 as long as the intermediate goods have valid pricing method.

7.2 Sensitivity analysis

This section contains the analysis associated to the computed sensitivity analysis of the thesis. The explanation of the phenomena observed bases in fundamental agricultural production economics (Debertin, 1986). More specifically, the observed changes are dependent on the law of diminishing returns and the concept of profit maximization.

7.2.1 Milk yield

An intuitive interpretation might be that the farm with the highest IOFC has the most to gain from an increased yield level of milk production. The empirical results of this study show that the true outcome is quite the opposite. The farm in Osby is the one with the highest IOFC of 2,10 SEK per Kg produced ECM in the baseline scenario. The sensitivity analysis performed in this study shows that the farmer in Osby is most vulnerable to shifting market conditions of the investigated farms. The Osby farm gains most from increased yield level of milk production in the form of highest total profit. However, Osby is the farm that has the lowest increase and the highest decrease as the yield levels shift.

The explanation of the observed phenomenon lies partly within the concept of diminishing returns for feeds (Debertin, 1986). The transformability of supplied feeds becomes lower as milk yield level increases. At the profit maximizing level of production the farmer loses money if production is increased further (ibid). Also the allowed share of by-products in feed ration declines and the share of forage increases as production level of milk increases. An indication of distance to profit maximizing level of production is given by feed cost per Kg ECM. Another explanation is the increased operational cost of forage and the restrictions that apply in terms of designing a feed ration (ibid). The effect is that the IOFC per kg ECM is diminishing at the Osby farm but still increasing at the other farms.

The reason behind the increasing IOFC of the other farms is a high proportion of farm grown feed. It leads to an amplified operational cost of produced feed as production increases (Debertin, 1986). Which alters the relative price ration between produced and purchased

feeds. It becomes cheaper to increase the share of purchased by-products than to increase feed production at farm level. It is the same reasoning as applies to the concept of marginal factor cost, MFC (ibid). Even if feed cost per produced kilogram of milk increases it might still be an optimal solution. This is true under the condition that the value marginal product, VMP, is higher or equal to MFC.

7.2.2 Changes in grain price

Since the farms evaluated are dairy farms they do not have the obvious possibility to terminate milk production or alter the number of cows in the short run (Flatén, 2001). Thus the farms have a predetermined need of feed to acquire. The choice to sell grain to a trader or to keep it as feed depends on current level of grain prices. If prices go up it would be rational for the farmer to sell grain at the higher price if he/she is able to cover feed requirements with purchased feed that is cheaper in comparison to grain produced at the farm. If however the grain prices drop he/she is keen to use part of his grain as feed. The choice is still determined by the MFC of each feed product as explained in chapter 3 (Debertin, 1986).

The high profit of the Osby farm originates from increased grain prices that exceed the increased operational cost of forage. Shadow price of forage increases if grain prices rise, since opportunity cost of grain production is a vital part of computing operational cost of forage (Debertin, 1986). This is a result of the resource allocation. At Vetlanda farm the land allocation is overweighed on feed production and the pattern is the opposite. The loss in profit due to the increased operational cost of forage exceeds the gain derived to the increased price of cereals.

The Alvesta farm is a special case. The farmer is beneficial from both a rise and a drop in grain prices. At the low level of grain prices the feed ration composition is unaltered. The increased total profit is generated from a lower operational cost of forage since the opportunity cost of grain production declines (Debertin, 1986). At the high grain price level the farmer alters his/hers feed strategy. It becomes more profitable to market produced cereals and the employment of by-products in the feed ration becomes more competitive. The operational cost of forage increases, but not to an extent that erases the profit increase generated by increased grain production.

7.2.3 Crop yield

The results and pattern of crop yield level changes strongly resembles the case of milk yield changes. The Osby farm reaches the highest profit. Still the farmer in Osby is the one most exposed to shifting market conditions. He/she has the largest decreases and smallest increases in profit as the crop yield level shifts.

Yield level of the crop production is essential as it determines the rate of operational cost for producing feed at the farm (Debertin, 1986). Basically, the operational cost declines if yield level increase and vice versa. However, the operational cost of grown feeds still increases if the yield level rises and grain prices are high enough.

Each farm increases profitability when crop yield increases and vice versa. The farms that have the biggest increase in profits are the farms with the highest share of farm grown feeds in the feed ration. The explanation is a lower opportunity cost of grown feed in combination with a decreased allocation of land for feed production since yields increase (Debertin, 1986). The Osby farm suffers the largest decrease of profit due to low crop yields. The reason is

lower profitability in grain production. Even if the farm enjoys benefit from a decreased operational cost of forage it does not compensate the decreased profitability in grain production.

Farms with fewer by-products have the largest reallocation of farm resources at high yield levels. On the other hand, farms with high usage of by-products are sensitive to decreased yield level due to an increase in operational cost of forage. Low amount of land allocated to forage and a decreased yield level results in major increases of land allocated for that purpose.

7.3 Discussion

This section intends to validate the findings of the thesis through comparison with existing knowledge delivered from previous studies. Possible differences between the findings of this study that conflict with the result of earlier studies are discussed. Potential differences may also be an outcome of different research methods.

The results of this study is in line with the existing notion that liquid stillage is a competitive feed option up to distances of 20 Swedish miles (Slätt & Swensson, 2009). The Vetlanda farm is located on the verge of this transportation distance. The Vetlanda farmer's tendency to employ liquid stillage in the baseline scenario is moderate. However as market conditions change it becomes an interesting feed option, see chapter 6. Gustafsson (2012) also stresses the competitiveness of liquid stillage as a feed option.

The results regarding utilization of HP-pulp indicates that the feed product is a competitive option for longer transportation distances than liquid stillage. The Vetlanda farm is employing HP-pulp in the feed ration of the baseline scenario to some extent. Observation is expected since the water content in the feed determines transportation cost. It could however be argued that employed amount in the case of Vetlanda should be larger. The prices of HP-pulp employed in this study are significantly higher compared to the prices of HP-pulp in an earlier study (Gustafsson et al., 2014). Chosen price level in this thesis is however set considering the disregarded investment perspective. It is vital the delimitation of investments does not create unreasonable results.

The tendencies displayed by the result of this study are supported by earlier studies (Buza et al., 2014; Gustafsson et al., 2014). The American study concludes that minimization of feed costs per se does not maximize IOFC per Kg ECM (Buza et al., 2014). The results of this study support this view since the empirical work shows that IOFC is correlated to profitability in grain production at the dairy farm. Furthermore, this study does not find any correlation between level of purchased feed and degree of profitability. However, the amount of employed by-product feeds does improve IOFC. This observation is also made by the American study, which also finds that utilization of by-products has the possibility to increase yields of milk production (Buza et al., 2014).

Further, the Swedish study enforces the opinion that complementary effects of employed feeds determine the profitability of feed rations (Gustafsson et al., 2014). The view is in line with the tendencies observed in this study. Also, the previous study concludes that it is the relative price ratio between different feed products that is the main determining factor for the choice of employed feeds, not the specific price levels (ibid). The explanation is prices of

feeds are intertwined and are affected by each other. These conclusions of the previous study validate the method and finding of the sensitivity analysis on this thesis.

Svensson (2013) supports the observed tendencies in modified resource allocation. Svensson concludes that more purchased feed leads to less allocated land for feed production. Svensson's findings confirm the findings of this study. Another factor affecting allocation of land for feed production is the quality and yield level of grown feeds (Alvemar, 2014). This study states that yield level of feed production is a vital factor in deduction of the operational cost. However, the quality aspect of feeds is disregarded in this study due to the desired scope of the study. Alvemar's finding is however indirectly visible in the reasoning applying to shifts in resource allocation observed in this study. Also the profitability of chosen feed strategy is dependent on constant surveillance of the herd's required feed quantity (Nygren, 2010). This in order to minimize costs associated with over-feeding as feed requirements of the herd shift over the year. This influence is also included in the delimitations of this study.

7.4 Sources of error

Possible causes of error margin in the optimization model may include differences in methods of data collection between sources, which may lead to inaccurate comparisons and results (Robson, 2011; Debertain, 1986). Due to volatility in market prices, the calculations may not be up to date and do not necessarily reflect the current situation on the market at the publication date.

The study intends to measure how by-products in the feed ration affect total profit. Thus, the chosen feed ration for a specific farm in the study must not be the one that minimizes feed costs (Debertain, 1986). It rather is the one that maximizes total profit of all farm operations. In reality, there may also be supplementary factors affecting the profitability as the feed ration changes, like the quality aspects of produced feeds (Patel, 2012; Alvemar, 2014). The study uses a personally developed mathematical program for feed ration design that enables examinations of the research questions at hand. The choice to use an old feed evaluation system as basis may lead to less effective feed rations in comparison than produced via Norfor (Gustafsson et al., 2014). Moreover, possible synergy effects of the feed nutritional contents may be disregarded since the employed feed evaluation system is a bit out of date. Also, the impact of the cow's need for minerals through the feed is overlooked (ibid).

At last, bear in mind the delimitations of the study. Assumptions that simplify the reality may have an impact on the validity of the study (Flaten, 2001). The model may also come up with feed rations that are not feasible in a real world situation due to unforeseen management costs. Finally, the interpretations of the results may be affected by the authors' previous knowledge and the possibility of alternative interpretations should not be ignored (Robson, 2011).

8 Conclusions

The study investigates the most prominent economic aspects of the possibility to incorporate by-products in the feed ration at a dairy farm. More specifically the two by-products: HP-pulp and liquid stillage. A dairy farm however has two production systems, which both are included in this study. The study recognizes that the key factor of determining profitability of employing feed by-products is the relative price ratio between available feeds, both produced and purchased. The specific price levels of feeds are not significantly affecting the chosen feed strategy. Also the competitiveness of by-products is dependent on the transportation distances from the distributing plants, which are not correlated to price level of feeds.

The study concludes that by-products are a preferable option in two out of three investigated case farms. The by-products contain valuable nutritional contents that are highly valued in the process of feed ration design, which is supported by previous studies (Buza et al, 2014; Gustafsson et al., 2014). Another implication is that an increased share of purchased feed enables reallocation of farm resources. This creates flexibility in resource allocation to the most profitable production system that increases total profit given the right conditions.

The case farm Osby is the farm located with the closest proximity to the distributing plants. Hence, the Osby farm enjoys the most beneficial prices of the two by-products. The consequence is that the Osby farm is the farm generating the biggest modified total profit of the investigated case farms. The profit of Osby sums up to 6 629 KSEK. This corresponds to a cost saving of 0,23 SEK per Kg ECM. The profit however does not incorporate costs for other purposes than feed acquisition. The profit of the Osby farm represents an increase of 739 SEK compared to the reference farm, which does not have the option to employ by-products.

Further, an adequate part of the empirical work is represented by a sensitivity analysis conducted within the scope of the study. The sensitivity analysis intends to provide the reader with a comprehensive understanding of chosen feed strategy and the implications for the farmer. The sensitivity analysis shows that the farm most vulnerable to shifting market conditions is the Osby farm. The Osby farm experiences the largest decreases and smallest increases in profit as the market conditions shift in a preferable direction. The interpretation is that Osby position itself in close proximity to the profit maximizing production level in both production systems (Debertin, 1986). The implication of an altered market situation therefor becomes more noticeable for Osby than the other case farms. The remaining case farms on the other hand suffers from a more restrained behavior in resource allocation, which explains the bigger differences in profit as market conditions change.

Finally, the opportunity to incorporate feed by-products in the feed strategy decision process has positive effects on both production systems of the dairy farm. However, the potential to increase profitability is dependent on the initial state of the dairy farm. Profitability of feeding operations is likely to increase. Further the profitability of grain production operations is also likely to increase, since a larger share of purchased feed frees up land to be reallocated for grain production of marketable cereals. The main determining factor of profitability associated with by-product utilization is however the transportation distances to the distributing plants.

9 Future research

This study needs to be complemented by other scholars with complementary research approaches and methods to be able to provide a more generalizable picture of the most rational behavior in feed strategy decisions.

Feed ration decisions influence both milk production level and milk composition, which affect milk revenue (McDonald et al., 2011; Chamberlain, 1996). Hence, it exists a research gap for profit maximization of feed rations with focus on feed by-product employment. The complementary nutritional effects of introduced feed by-products may be more accurately valued if the research approach of this study is combined with the Norfor feed evaluation system (Gustafsson, 2012; Gustafsson et al., 2014). Also the complementary nutritional effects of by-products may increase the nutritional value of farm grown feeds since new feed ration compositions are enabled. A consolidation of the Norfor System may lead to enhancement of competitiveness for the feed by-products (ibid).

The authors identify a need for research on the relationship between different feeds, their synergies and the effect on milk quality in terms of fat and protein content. A deeper understanding of the phenomenon would enable more valid economic valuations of feed ration composition. It is also of interest financial implications of storage losses and quality deficiencies.

Other applications of the research conducted within this study, is to evaluate other alternative feed by-products. The necessity for profitable feed strategies creates an interest among farmers to scrutiny the possibility of utilizing by-product feeds from the food processing industry. Another example is to employ the developed model of this study to incorporate feed quality aspects in the feed strategy decision process, in future research. It is the quality aspects of forage production that is specifically interesting (Patel, 2012; Alvemar, 2014)

Bibliography

Literature and publications

- Alvemar, H., 2014. *Controlled traffic for grass silage production; an economic evaluation for dairy farmers*, Department of Economics, Swedish University of Agricultural Sciences, Uppsala (ISSN 1401-4084).
- Andersson, C., and Gotting, M., 2011. Policies affecting the competitiveness of dairy production in Sweden, Denmark and Germany. Department of Economics, Swedish University of Agricultural Sciences, Uppsala (ISSN 1401-4084)
- Anderson, D., Sweeney, D., Williams, T., Camm, J., Cochran, J., Fry, M., Ohlmann, J., 2014. *An introduction to management studies: Quantitative approaches to decision making*. Cengage Learning, Boston (ISBN 978-1-111-82361-0).
- Bertilsson, J., Burstedt, E., 1983. Effects of conservation method and stage of maturity upon the feeding value of forages to dairy cows. *Swedish Journal of Agricultural Research*, 1983 Report 104 v13, pp189-200, Uppsala (ISBN 91-576-1500-4).
- Bergknut, P., Elmgren-Warberg, J., Hentzel, M., 1993. *Investering i teori och praktik*, Studentlitteratur, Lund.
- Bryman, A., 2008. *Social research methods*, Oxford University Press, Oxford (ISBN 978-0-19-920259-9).
- Buza, M. H., Holden, L.A., White, R.A., Ishler, V.A., 2014. Evaluating the effect of ration composition on income over feed cost and milk yield. *Journal of Dairy Science*, Volume 97, Issue 5, pp 3073-3080.
- Chamberlain, A., and Wilkinson, J., 1996. *Feeding the dairy cow*. Chalcombe Publications, Welton (ISBN 0 948 617 32 2)
- Debertin, D., 1986. *Agricultural production economics*. Macmillan Publishers, New York (ISBN 0-02-328060-3).
- Ejvegård, R., 2009. *Vetenskaplig metod*, Studentlitteratur, Lund (ISBN 978-91-44-05474-2).
- Ekman, S., 1995. *Mjölkgårdens anpassning till EU*, Swedish University of Agricultural Sciences, Uppsala (91-576-5049-7).
- Flaten, O., 2001. *Økonomiske analyser av tilpassinger i norsk mjølkeproduksjon*. Norges landbrukshøgskole, Ås (ISBN 82-575-0449-1).
- Frankow-Lindberg, B., 2013. Intensivt skördade vallar. *Sverigeförsöken 2013 Försöksrapport Animaliebältet*, pp 49-53.

- Freeze, B. & Richards, T., 1992. Lactation Curve Estimation for Use in Economic Optimization. *Journal of Dairy Science* Vol. 75, No. 11, 1992 pp 2984-2989.
- Gunnarsson, F., 2002. *Economic consequences of VMS technology at farm level*. Department of Economics, Swedish University of Agricultural Sciences, Uppsala (ISSN 1401-405X).
- Gustafsson, A., 2012. *Närproducerat foder fullt ut*. Svensk Mjolk.
- Gustafsson, A., Persson, A.-T., Lovang, U., 2014. *Olika strategier för närproducerat foder på mjölkgårdar*. Växa Sverige, Rapport nr: 2.
- Hazell, P., Norton, R., 1986. *Mathematical programming for economic analysis an agriculture*. Macmillan Publishing Company, New York (ISBN 0-02-947930-4).
- Klein, K., Hironaka, R., Heller, C., Freeze, B., 1986. Profit-Maximizing Linear Program Model for Dairy Cattle, *Journal of Dairy Science* Vol. 69, No. 4, pp 1070-1080.
- Kokkontrollen, 2015. *Avkastning kg ECM per ko och dag under olika laktationsmånader, kontrollår 2014*, Rapport 5. Unpublished material, Eskilstuna.
- LRF Mjolk:
1. *Mejerimarknadsrapport nr 6 2014*, 2014. LRF Mjolk.
 2. *Mjölkekonominrapport nr 4 2014*, 2014. LRF Mjolk.
 - *Mjölkrapporten nr 1 Mars 2015*, 2015. LRF Mjolk.
- Lundgren J., Rönnqvist M., Värbrand P., 2001. *Linjär och icke-linjär optimering*. Studentlitteratur, Lund (ISBN 91-44-01798-7)
- Lärn-Nilsson, J. 2007. *Naturbrukets husdjur Del 1*. Bokförlaget Natur och Kultur, Stockholm (ISBN 978-91-27-35632-0).
- Magnusson, A.-T., Bertilsson, J., Everitt, B., Lindberg, J.-E., Sanne, S., Spörndly, R., 1990. Uvärdering av AAT/PBV-systemet för användning i mjölkproduktionen. *Konsulentavdelningens rapporter, Husdjur, nr 68*, Sveriges lantbruksuniversitet, Uppsala.
- McDonald, P., Edwards, R.A., Greenhalgh, J.F.D., Morgan, C.A., Sinclair, L.A., Wilkinson, R.G., 2011. *Animal nutrition*. Pearson Education, Harlow (978-1-4082-0423-8).
- National research council (NRC), 1988. *Nutrient requirements of dairy cattle*. National Academic Press, Washington D.C.
- Nilsson, T., 2006. *How do I build a functional barn for loose-housed dairy cows?* Swedish University of Agricultural Sciences, Alnarp

- Nycander, L., 1989. *Estimation of feed intake in dairy cattle measuring the neutral detergent fiber (NDF) and indigestible neutral detergent fiber (INDF)*, Department of Animal Nutrition and Management, Swedish University of Agricultural Sciences, thesis no 11.
- Nygren, R., 2010. *An Analysis of feed costs in dairy production*. Department of Economics, Swedish University of Agricultural Sciences, Uppsala (ISSN 1401-4084).
- Oliver, P., 2010. *Student's guide to research ethics*. McGraw-Hill Education, Berkshire (ISBN 978-0-33-523797-5).
- Patel M., 2012. *Effects of increasing the proportion of high-quality grass silage in the diet of dairy cows*. Department of Animal Nutrition and Management, Swedish University of Agricultural Sciences, Uppsala (ISBN 978-91-576-7727-3).
- Pindyck, R., Rubinfeld, D., 2009. *Microeconomics*. Pearson Education, Upper Saddle River, New Jersey (ISBN 978-0-13-713335-2).
- Pidd, M., 2009. *Tools for thinking; Modelling in management science*, A John Wiley and Sons, Ltd, Chichester (ISBN 978-0-470-72142-1).
- Robson, C., 2011. *Real world research*, John Wiley & Sons Ltd, Chichester, United Kingdom (ISBN 978-1-4051-82409).
- Slätt, S., Swensson, C., 2008. *Hur kan blöt vetedrank, lagras, hanteras och utfodras till mjölkkor*. Swedish University of Agricultural Sciences, Alnarp (ISSN 1401-4084).
- Spörndly, R., 2003. *Fodertabeller för idisslare*, Rapport 257, Department of Animal Nutrition and Management, Swedish University of Agricultural Sciences, Uppsala (ISRN SLU-HUV-R-257-SE)
- Svensson, S., 2013. *Feed and crop productions strategies for dairy cows; a case study focusing on the link between crop and milk production*. Department of Economics, Swedish University of Agricultural Sciences, Uppsala (ISSN 1401-4084).
- The Swedish Board of Agriculture (SJV), 2012. *Marknadsöversikt – Mjolk och mejeriprodukter, 2012*. Jordbruksverket, (ISSN 1102-3007, ISRN SJV-R-12/7-SE)
- Thurén, T., 1997. *Källkritik*. Liber, Stockholm (ISBN 91-21-16820-2).
- Turban, E., Aronson, J., Bolloju, N., 2001. *Decision support systems and intelligent systems*. Prentice Hall International, Upper saddle river, N.J., (ISBN 0-13-032723-9).
- Volden, H., 2011. *Norfor – The Nordic feed evaluation system*. EAAP publication No. 130. Wageningen Academic Publishers (ISBN: 978-90-8686-162-0)
- Wallman, M., Cederberg, C., Florén, B., Strid, I., 2010. *Life cycle assessment of locally produced feed for dairy cows*, Department of Energy and Technology, Swedish University of Agricultural Sciences, Uppsala (ISSN 1654-9406)

- Wiktorsson, H., 1988. Nya rekommendationer för utfodring av fett till mjölkkor. *Svensk husdjursskötsel nr 152*, Eskilstuna.
- Wolf, C.A., 2010. Understanding the milk-to-feed price ratio as a proxy for dairy farm profitability. *Journal of Dairy Science*, Volume 93, Issue 10, pp 4942-4948.
- Yin, R.K., 2003. *Case study research: Design & methods*. Sage Publications. London (ISBN 0-7619-2553-8).

Internet

Agriwise, <http://www.agriwise.org/>

1. Databoken, 2015-02-25
<http://www.agriwise.org/Databoken/databok2k15/kalkyler2015/kalkyler.aspx>
2. Om Agriwise 2015-06-02
<http://www.agriwise.org/omagriwise/index.html>

Arla, <http://www.arla.se>

1. Arlas historia , 2015-02-03
<http://www.arla.se/om-arla/arlas-historia/>
2. Arlas räknesnurra, 2015-05-19.
<http://www.arla.com/sv/agare/raknesnuran/>

Fonterra, <http://www.fonterra.com>

1. The global dairy industry, 2015-02-10
<http://www.fonterra.com/global/en/Financial/Global+Dairy+Industry>
2. About Fonterra, 2015-02-10
<http://www.fonterra.com/global/en/About/>

GDT, Global dairy trade, <https://www.globaldairytrade.com/>

Skim Milk Powder Prices, 5 years, 2015-03-30
<https://www.globaldairytrade.info/en/product-results/skim-milk-powder/>

SJV, The Swedish Board of Agriculture, <http://www.sjv.se>

1. Antal företag med nötkreatur i juni 2014, 2015-02-05
http://www.jordbruksverket.se/webdav/files/SJV/Amnesomraden/Statistik,%20fakta/Husdjur/JO20/JO20SM1403/JO20SM1403_tabeller2.htm
(JO 20 SM 1403)
2. Antal företag och nötkreatur av olika slag i riket i juni 2011, 2015-02-05
http://www.jordbruksverket.se/webdav/files/SJV/Amnesomraden/Statistik,%20fakta/Annan%20statistik/Statistikrapport/Statistikrapport2012_3/201203._tabeller2.htm
(Statistikrapport 2012:03)
3. När dina nötkreatur är ute eller på bete, 2015-05-22
http://www.jordbruksverket.se/amnesomraden/djur/olikaslagsdjur/notkreatur/utevistels_eochbetesgang.4.4b00b7db11efe58e66b8000308.html
4. Prisindex och priser på livsmedelsområdet, 2015-05-21
http://www.jordbruksverket.se/webdav/files/SJV/Amnesomraden/Statistik,%20fakta/Priser%20och%20prisindex/JO49/JO49SM1505/JO49SM1505_tabeller8.htm
(JO 49 SM 1505)

Government Offices of Sweden, <http://www.regeringen.se/>

Handlingsplan för Sveriges mjölkbönder, 2015-05-26
<http://www.regeringen.se/pressmeddelanden/2015/05/handlingsplan-for-sveriges-mjolkbonder/>

Lantmännen, <http://www.lantmannen.se/>

Prislista för foderprodukter till nötkreatur, 2015-02-24
<https://www.lantmannenlantbruk.se/sv/Foder/Not/>

SLU, Swedish University of Agricultural Sciences, www.slu.se

Feed tables for ruminants, 2015-03-09
<http://www.slu.se/sv/institutioner/husdjurens-utfodring-ward/verktyg/fodertabeller/fodertabell-for-idisslare/>

Svenskt Kött, www.svensktkott.se

Svensk Låglandsboskap eller Svensk Holstein, 2015-08-28
<http://www.svensktkott.se/om-kott/kott-och-miljo/uppfodning/not/mjolkkoraser/svensk-laglandsboskap-eller-svensk-holstein/>

Växa Sverige, www.vxa.se

Statistik Foderanalyser Norfor, skördeår 2014, 2015-04-28

http://vxa.se/Documents/Foder/Sk%C3%B6rde%C3%A5r2014/Omr%C3%A5de_C_2014%5b1%5d.pdf

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This appendix consists of tree calculation sheets made by Rolf Spörndly at the Department of Animal Nutrition and Management, SLU.

Figure A1.1 Calculation of total feed consumption – Feed ration for 8 000 kg ECM

Calculation of total feed consumption – Feed ration for 10 000 kg ECM																									
Yield, kg ECM		10279		Roughage % : 61			KRAV%:		0		Starch% :		149		Number of cows:		300		Stable period, days:		250				
Lact. month		1		2		3		4		5		6		7		8		9		10		sin		sin	
ECM		41		41		38		38		36		34		31		29		26		23		0		0	
kg DM forage	8	8	8	8	8	8	8	8	8	8	8	10	10	10	10	10	10	10	10	10	6	6	6	6	
Kg DM maize	4	4	4	4	4	4	4	4	4	4	4	2	2	2	2	2	2	2	2	2	3	3	3	3	
kg straw																									
kg cereals	6	6	6	5,5	5,5	5,5	5,5	5	4	4	4	3,5	3	3	3	3	2,5	2,5	2,5	2,5	0,5	0,5	0,5	0,5	
kg conc.	7	7	7	6	6	6	6	5	4	4	4	3,8	3	3	3	3	2,5	2,5	2,5	2,5	0,5	0,5	0,5	0,5	
g mineral feed	50	50	50	50	50	100	100	100	100	100	100	100	100	120	150	200	200	200	200	200	200	200	200	200	
Total kg ts		23,6	23,6	22,2	22,2	21,4	20,5	19,2	18,6	17,4	17,0	8,7	9,6												
MI/kg ts	12,4	12,4	12,3	12,3	12,2	12,1	12,0	11,9	11,8	11,7	9,5	9,9	9,9	9,9	9,5	9,9	9,9	9,9	9,9	9,9	9,9	9,9	9,9	9,9	
AAT/MJ	8,1	8,1	8,0	8,0	7,8	7,8	7,7	7,6	7,5	7,4	6,9	7,2	7,2	7,2	6,9	7,2	7,2	7,2	7,2	7,2	7,2	7,2	7,2	7,2	
PBV, g	218	218	177	177	122	108	108	274	244	216	24	38	38	38	24	38	38	38	38	38	38	38	38	38	
% MI	102	102	101	101	101	100	100	101	101	101	102	116	117	117	116	117	117	117	117	117	117	117	117	117	
% AAT	108	108	106	106	104	103	101	101	101	100	105	111	111	111	105	111	111	111	111	111	111	111	111	111	
% rp	17	17	17	17	16	16	16	16	16	16	12	12	12	12	12	12	12	12	12	12	12	12	12	12	
% Roughage	51	51	54	54	56	59	63	65	69	71	98	89	89	89	98	89	89	89	89	89	89	89	89	89	
% KRAV	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0		
% Starch	177	177	175	175	180	175	160	127	119	121	2	30	30	30	2	30	30	30	30	30	30	30	30	30	
% Ca	100	100	99	99	104	104	107	117	118	117	172	184	184	184	172	184	184	184	184	184	184	184	184	184	
% P	104	104	102	102	104	103	101	104	103	99	102	105	105	105	102	105	105	105	105	105	105	105	105	105	
Total / year		Quantity	Price (SEK)	Sum	DMI content			MJ	AAT	PBV	rp	Ca	P	Roughage	Starch	KRAV									
ECM	10279	3	30836					/kg DM	g/kg DM	g/kg DM	g/kg DM	g/kg DM	g/kg DM	%	%	%									
kg DM forage	2989	1,3	3886	1	11			72	27	150	6	2,8	100	0	0	0									
Kg DM maize	1037	1,5	1556	1	11			82	-55	90	2,4	2,3	100	223	0	0									
kg straw	183	1	183	0,85	6,6			55	-54	40	3,3	1,1	100	0	0	0									
kg cereals	1449	1,9	2753	0,87	13,6			93	-31	122	0,3	3,7	0	581	0	0									
kg conc.	1504	3,5	5263	0,9	14			153	61	290	11	5,6	0	38	0	0									
g mineral feed	0		0	1							230	60	0	100	0	0									
Total kg DM	6831				Feed cost, SEK/kg ECM:			1,35																	

Calculation of total feed consumption – Feed ration for 12 000 kg ECM																							
Yield, kg ECM:	12048		Roughage %: 55				KRAV%:				0	Starch%:				19	Number of cows:				300		
Lact. month	1	2	3	4	5	6	7	8	9	10	sin	sin	Stable period, days:				250						
ECM	47	47	45	45	40	40	38	35	30	28	0	0	Sum, per herd				per year	per stable per					
kg DM forage	6	6	6	6	7	7	8	8	10	10	6	6	kg DM forage				786 900	538 973					
Kg DM maize	6	6	6	6	5	5	4	4	2	2			Kg DM maize				420 900	288 288					
kg straw											3	3	kg straw				54 900	37 603					
kg cereals	8	8	7,5	7,5	6,5	6,5	6,5	5	4,5	4,3		0,5	kg cereals				592 920	406 110					
kg conc.	8	8	7,5	7,5	6	6	5	5	3,5	3,3		0,5	kg conc.				551 745	377 908					
g mineral feed	100	100	100	100	100	100	100	100	100	120	150	200	g mineral feed				12 536	8 586					
Total kg ts	26,3	26,3	25,4	25,4	23,2	23,2	22,3	21,0	19,2	18,8	8,7	9,6											
MI/kg ts	12,5	12,5	12,4	12,4	12,3	12,3	12,2	12,1	12,0	11,9	9,5	9,9											
AAT/MI	8,2	8,2	8,1	8,1	8,0	8,0	7,8	7,9	7,5	7,5	6,9	7,2											
PBV, g	55	55	41	41	68	68	95	136	231	225	24	38											
% MF	103	103	102	102	101	101	101	101	102	101	116	117											
% AAT	110	110	109	109	106	106	103	104	101	100	105	111											
% rp	17	17	17	17	16	16	16	16	16	16	12	12											
% Roughage	46	46	47	47	52	52	54	57	63	64	98	89											
% KRAV	0	0	0	0	0	0	0	0	0	0	0	0											
% Starch	22	22	22	22	20	20	20	18	15	15	2	5											
% Ca	100	100	100	100	101	101	100	106	111	111	172	184											
% P	108	108	107	107	105	105	104	104	104	99	102	105											
Total / year	Quantity	Price (SEK)	Sum	DM content				MI	AAT	PBV	rp	Ca	P	Roughage	Starch	KRAV							
ECM	12048	3	36143					/kg DM	g/kg DM	g/kg DM	g/kg DM	g/kg DM	g/kg DM	%	%	%							
kg DM forage	2623	1,3	3410	1				11	72	27	150	6	2,8	100	0	0							
Kg DM maize	1403	1,5	2105	1				11	82	-55	90	2,4	2,3	100	22,3	0							
kg straw	183	1	183	0,85				6,6	55	-54	40	3,3	1,1	100	0	0							
kg cereals	1976	1,9	3755	0,87				13,6	93	-31	122	0,3	3,7	0	58,1	0							
kg conc.	1839	3,5	6437	0,9				14	153	61	290	11	5,6	0	3,8	0							
g mineral feed	42	8	334	1								230	60	0	100	0							
Total kg DM	7598			Feed cost, SEK/kg ECM:				1,35					19 919										
													55										
				IOFC, SEK/cow and year:																			
				IOFC, SEK/cow and day:																			

Figure A1.3 Calculation of total feed consumption – Feed ration for 12 000 kg ECM

Appendix 2: Price lists of by products

Table A2.1 Price list of Hp-pulp

Prislista kr kg/ts			
Postnummer		Bulk	Hård-Pack
- 210 00	249 99	1,10	1,40
- 250 00	299 99	1,20	1,50
- 300 00	310 49	1,30	1,60
- 310 50	311 99	1,40	1,70
- 312 00	313 99	1,30	1,60
- 314 00	342 99	1,40	1,70
- 343 00	349 99	1,30	1,60
- 350 00	373 99	1,40	1,70
- 374 00	379 99	1,30	1,60
- 380 00	381 99	1,60	1,90
- 382 00	382 99	1,40	1,70
- 383 00	384 99	1,50	1,80
- 385 00	385 99	1,40	1,70
- 386 00	387 99	1,60	1,90
- 388 00	399 99	1,40	1,70
- 400 00	430 19	1,40	1,70
- 430 20	432 69	1,50	1,80
- 432 70	432 95	1,40	1,70
- 432 96	439 99	1,50	1,80
- 440 00	499 99	1,70	2,00
- 500 00	519 99	1,60	1,90
- 520 00	529 99	1,70	2,00
- 530 00	542 99	1,80	2,10
- 543 00	544 99	1,70	2,00
- 545 00	549 99	1,80	2,10
- 550 00	566 99	1,60	1,90
- 567 00	570 29	1,50	1,80
- 570 30	571 99	1,60	1,90
- 572 00	573 99	1,70	2,00
- 574 00	575 99	1,60	1,90
- 576 00	576 99	1,50	1,80
- 577 00	579 99	1,60	1,90
- 580 00	585 99	1,90	*
- 586 00	590 79	1,80	*
- 590 80	590 81	1,70	2,00
- 590 82	597 99	1,80	*
- 598 00	598 99	1,70	*
- 599 00	619 99	1,90	*
- 630 00	719 99	2,00	*
- Övriga postnummer		Offertpris	Offertpris

Tillägg Lastväxlare 20 kr /ton HP-Massa.

* Vi kommer ej att leverera Hård-Pack i dessa postnummerområden.

Table A2.2. Price list of liquid stillage.



Vetedrankpris inklusive frakt 2014 - 2015

Avstånd	Ekipage storlek	Leverans volym	Pris fritt gård 2014-2015
0,01 - 10 km	Under 13,1	0 - 13,0 ton	90,50 kr
0,01 - 10 km	Hel bil	13,1 - 24,9 ton	87,50 kr
0,01 - 10 km	Hel släp	25,0 - 34,9 ton	81,50 kr
0,01 - 10 km	Helt ekipage	Över 42,0 ton	78,50 kr
10,01 - 20 km	Under 13,1	0 - 13,0 ton	93,00 kr
10,01 - 20 km	Hel bil	13,1 - 24,9 ton	90,00 kr
10,01 - 20 km	Hel släp	25,0 - 34,9 ton	84,00 kr
10,01 - 20 km	Helt ekipage	Över 42,0 ton	81,00 kr
20,01 - 30 km	Under 13,1	0 - 13,0 ton	96,00 kr
20,01 - 30 km	Hel bil	13,1 - 24,9 ton	93,00 kr
20,01 - 30 km	Hel släp	25,0 - 34,9 ton	87,00 kr
20,01 - 30 km	Helt ekipage	Över 42,0 ton	84,00 kr
30,01 - 40 km	Under 13,1	0 - 13,0 ton	99,50 kr
30,01 - 40 km	Hel bil	13,1 - 24,9 ton	96,50 kr
30,01 - 40 km	Hel släp	25,0 - 34,9 ton	90,50 kr
30,01 - 40 km	Helt ekipage	Över 42,0 ton	87,50 kr
40,01 - 50 km	Under 13,1	0 - 13,0 ton	103,00 kr
40,01 - 50 km	Hel bil	13,1 - 24,9 ton	100,00 kr
40,01 - 50 km	Hel släp	25,0 - 34,9 ton	94,00 kr
40,01 - 50 km	Helt ekipage	Över 42,0 ton	91,00 kr
50,01 - 60 km	Under 13,1	0 - 13,0 ton	107,00 kr
50,01 - 60 km	Hel bil	13,1 - 24,9 ton	104,00 kr
50,01 - 60 km	Hel släp	25,0 - 34,9 ton	98,00 kr
50,01 - 60 km	Helt ekipage	Över 42,0 ton	94,00 kr
60,01 - 70 km	Under 13,1	0 - 13,0 ton	111,00 kr
60,01 - 70 km	Hel bil	13,1 - 24,9 ton	108,00 kr
60,01 - 70 km	Hel släp	25,0 - 34,9 ton	102,00 kr
60,01 - 70 km	Helt ekipage	Över 42,0 ton	98,00 kr
70,01 - 80 km	Under 13,1	0 - 13,0 ton	115,00 kr
70,01 - 80 km	Hel bil	13,1 - 24,9 ton	112,00 kr
70,01 - 80 km	Hel släp	25,0 - 34,9 ton	106,00 kr
70,01 - 80 km	Helt ekipage	Över 42,0 ton	102,00 kr
80,01 - 85 km	Under 13,1	0 - 13,0 ton	119,00 kr
80,01 - 85 km	Hel bil	13,1 - 24,9 ton	116,00 kr
80,01 - 85 km	Hel släp	25,0 - 34,9 ton	110,00 kr
80,01 - 85 km	Helt ekipage	Över 42,0 ton	106,00 kr
85,01 - 90 km	Under 13,1	0 - 13,0 ton	124,00 kr
85,01 - 90 km	Hel bil	13,1 - 24,9 ton	121,00 kr
85,01 - 90 km	Hel släp	25,0 - 34,9 ton	114,00 kr
85,01 - 90 km	Helt ekipage	Över 42,0 ton	110,00 kr

Table A2.3. Price list of liquid stillage (continued).

Vetedrankpris inklusive frakt 2014 - 2015

Avstånd	Ekipage storlek	Leverans volym	Pris fritt gård 2014-2015
90,01 - 95 km	Under 13,1	0 - 13,0 ton	127,00 kr
90,01 - 95 km	Hel bil	13,1 - 24,9 ton	125,00 kr
90,01 - 95 km	Hel släp	25,0 - 34,9 ton	119,00 kr
90,01 - 95 km	Helt ekipage	Över 42,0 ton	114,00 kr
95,01 - 100 km	Under 13,1	0 - 13,0 ton	131,00 kr
95,01 - 100 km	Hel bil	13,1 - 24,9 ton	129,00 kr
95,01 - 100 km	Hel släp	25,0 - 34,9 ton	123,00 kr
95,01 - 100 km	Helt ekipage	Över 42,0 ton	118,00 kr
100,01 - 105 km	Endast leverans av helt ekipage	Över 42,0 ton	121,00 kr
105,01 - 110 km	Endast leverans av helt ekipage	Över 42,0 ton	124,00 kr
110,01 - 115 km	Endast leverans av helt ekipage	Över 42,0 ton	127,00 kr
115,01 - 120 km	Endast leverans av helt ekipage	Över 42,0 ton	130,00 kr
120,01 - 125 km	Endast leverans av helt ekipage	Över 42,0 ton	133,00 kr
125,01 - 130 km	Endast leverans av helt ekipage	Över 42,0 ton	136,00 kr
130,01 - 135 km	Endast leverans av helt ekipage	Över 42,0 ton	139,00 kr
135,01 - 140 km	Endast leverans av helt ekipage	Över 42,0 ton	142,00 kr
140,01 - 145 km	Endast leverans av helt ekipage	Över 42,0 ton	145,00 kr
145,01 - 150 km	Endast leverans av helt ekipage	Över 42,0 ton	148,00 kr
150,01 - 155 km	Endast leverans av helt ekipage	Över 42,0 ton	151,00 kr
155,01 - 160 km	Endast leverans av helt ekipage	Över 42,0 ton	154,00 kr
160,01 - 165 km	Endast leverans av helt ekipage	Över 42,0 ton	157,00 kr
165,01 - 170 km	Endast leverans av helt ekipage	Över 42,0 ton	160,00 kr
170,01 - 175 km	Endast leverans av helt ekipage	Över 42,0 ton	163,00 kr
175,01 - 180 km	Endast leverans av helt ekipage	Över 42,0 ton	166,00 kr
180,01 - 185 km	Endast leverans av helt ekipage	Över 42,0 ton	169,00 kr
185,01 - 190 km	Endast leverans av helt ekipage	Över 42,0 ton	172,00 kr
190,01 - 195 km	Endast leverans av helt ekipage	Över 42,0 ton	175,00 kr
195,01 - 200 km	Endast leverans av helt ekipage	Över 42,0 ton	178,00 kr

För leveranser under 13 ton under 10 mil och för leveranser
under 42 ton på avstånd över 10 mil till kommer minifrakt.
Vid flyttning mellan olika tankar på fastigheten tillkommer 150 kr per stopp.
TAC förbehåller sig rätten att kompensera för drivmedelsförändringar
som sker under avtalstiden.

Appendix 3: Overview of constraints

Figure A3:1 visualizes the complexity of the relationships between the constraints. The main constraint regarding crop production, including feed production, is crop rotation. It has significance for production cost and yield levels. The major constraints of the thesis are nutritional requirements constraints, which determine flexibility in feed ration design. the nutritional constraints are developed from the major nutritional constraint in equation (8) to capture the complex nature of feed strategies and their impact on farm profitability.

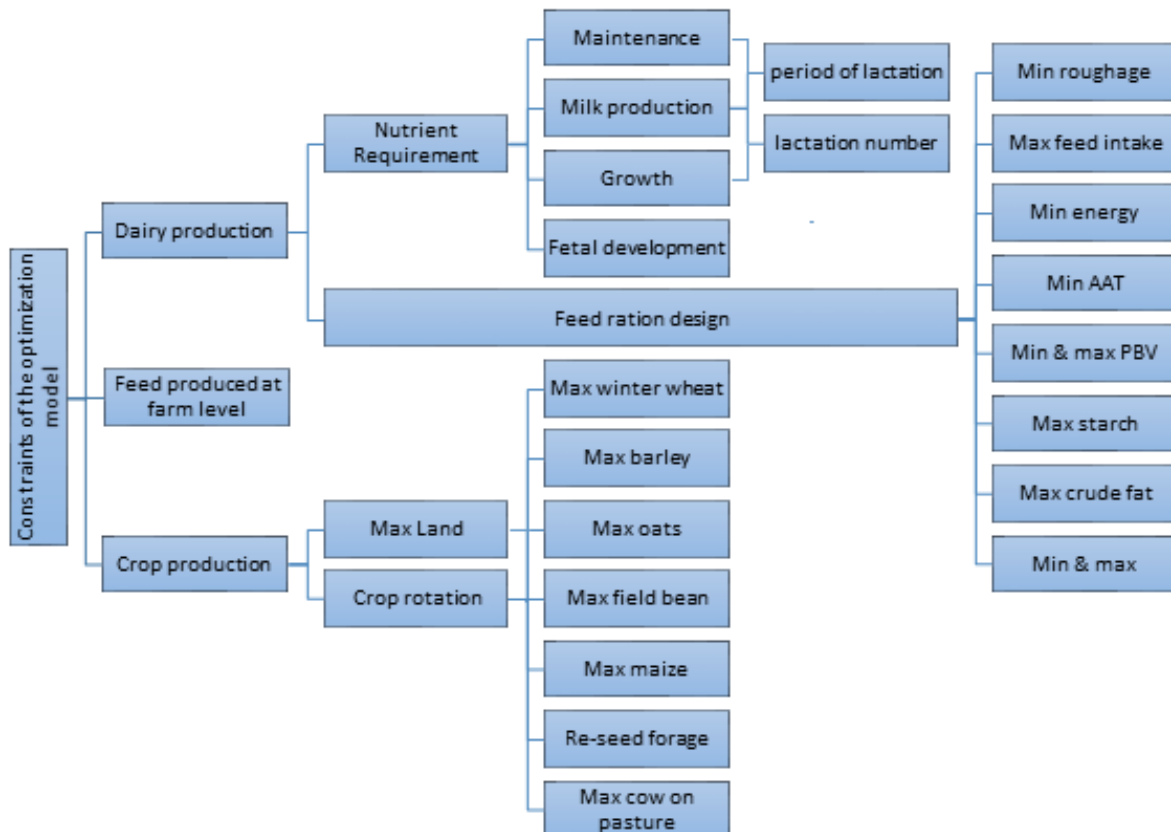


Figure A3.1. An overview of the constraints in the model.

Appendix 4: Complementary results

Reference farm

Table A4.1 Revenues and costs which gives income over feed costs for a dairy cow at the Reference farm

Reference farm	Kg ECM		Price	Sum
Milk yield	10 019		3,07	30 751
Feed ration	Kg DM	% of Kg DM	Price	Sum
Forage	2 613	36%	-2,19	-5 730
Natural pasture	308	4%	0,51	157
Barley	2 198	30%	-1,36	-2 982
Oats	1 615	22%	-1,32	-2 139
Expro	495	7%	-2,72	-1 348
Total feed cost per cow			SEK/year	12 043
IOFC per cow and year			SEK/year	18 708
IOFC per cow and day			SEK/day	51
IOFC per Kg ECM			SEK/Kg ECM	1,9
Feed cost			SEK/ Kg ECM	1,20
Total work in crop production			hours	1 471
Work in crop production for feed			hours	1 018

Osby farm

Table A4.2 Revenues and costs which gives income over feed costs for a dairy cow at Osby farm.

Osby farm	Kg ECM		Price	Sum
Milk yield	10 019		3,07	30 751
Feed ration	Kg DM	% of Kg DM	Price	Sum
Forage	2 346	34%	-1,68	-3 949
Natural pasture	308	4%	0,51	157
Barley	571	8%	-1,36	-775
HP-pulp	2 672	39%	-1,50	-4 009
Stillage	956	14%	-1,16	-1 110
Total feed cost per cow			SEK/year	9 686
IOFC per cow and year			SEK/year	21 065
IOFC per cow and day			SEK/day	57,6
IOFC per Kg ECM			SEK/Kg ECM	2,10
Feed cost			SEK/ Kg ECM	0,97
Total work in crop production			hours	1447
Work in crop production for feed			hours	941

Alvesta farm

Table A4.3 Revenues and costs which gives income over feed costs for a dairy cow at Alvesta farm.

Alvesta farm	Kg ECM		Price	Sum
Milk yield	10 019		3,07	30 751
Feed ration	Kg DM	% of Kg DM	Price	Sum
Forage	2 489	36%	-2,19	-5 459
Natural pasture	308	4%	0,51	157
Barley	2 067	30%	-1,36	-2 805
HP-pulp	1 237	18%	-1,70	-2 103
Stillage	552	8%	-1,68	-927
Expro	216	3%	-2,72	-588
Total feed cost per cow			SEK/year	11 725
IOFC per cow and year			SEK/year	19 026
IOFC per cow and day			SEK/day	52,0
IOFC per Kg ECM			SEK/Kg ECM	1,90
Feed cost			SEK/ Kg ECM	1,17
Total work in crop production			hours	1460
Work in crop production for feed			hours	975

Vetlanda farm

Table A4.4 Revenues and costs which gives income over feed costs for a dairy cow at Vetlanda farm.

Vetlanda farm	Kg ECM		Price	Sum
Milk yield	10 019		3,07	30 751
Feed ration	Kg DM	% of Kg DM	Price	Sum
Forage	2 591	37%	-2,19	-5 682
Natural pasture	308	4%	0,51	157
Barley	1 864	26%	-1,36	-2 529
Oats	1 524	22%	-1,32	-2 019
HP-pulp	220	3%	-1,90	-418
Expro	566	8%	-2,72	-1 542
Total feed cost per cow			SEK/year	12 033
IOFC per cow and year			SEK/year	18 718
IOFC per cow and day			SEK/day	51,1
IOFC per Kg ECM			SEK/Kg ECM	1,87
Feed cost			SEK/ Kg ECM	1,20
Total work in crop production			hours	1469
Work in crop production for feed			hours	1011

Feed rations

Table A4.5. Feed rations chosen by the optimization model in each scenario.

	Feed ration Kg DM per cow and day							
	Forage	N. pasture	Maize	Barley	Oats	HP-pulp	Stillage	Expro
Low milk yield								
Reference	6,8	0,8	0,0	4,4	5,5	0,0	0,0	0,8
Osby	6,1	0,8	0,0	0,9	0,0	6,5	2,2	0,0
Alvesta	6,3	0,8	0,0	2,6	0,0	4,8	1,8	0,2
Vetlanda	6,6	0,8	0,0	1,9	4,9	1,6	0,0	1,4
Normal milk yield								
Reference	7,1	0,8	0,0	6,0	4,4	0,0	0,0	1,4
Osby	6,4	0,8	0,0	1,6	0,0	7,3	2,6	0,0
Alvesta	6,8	0,8	0,0	5,6	0,0	3,4	1,5	0,6
Vetlanda	7,1	0,8	0,0	5,1	4,2	0,6	0,0	1,5
High milk yield								
Reference	6,6	0,8	1,7	4,4	6,0	0,0	0,0	1,9
Osby	6,7	0,8	0,0	2,2	0,0	8,1	3,0	0,0
Alvesta	7,3	0,8	0,0	8,7	0,0	1,9	1,3	0,9
Vetlanda	7,4	0,8	0,0	8,6	1,0	1,2	0,9	1,2
Low grain price								
Reference	7,1	0,8	0,0	6,0	4,4	0,0	0,0	1,3
Osby	6,3	0,8	0,0	0,0	0,0	8,7	2,9	0,0
Alvesta	6,6	0,8	0,0	3,3	0,0	5,7	2,1	0,2
Vetlanda	7,1	0,8	0,0	5,1	4,1	0,6	0,0	1,5
High grain price								
Reference	7,1	0,8	0,0	6,0	4,4	0,0	0,0	1,3
Osby	6,4	0,8	0,0	1,6	0,0	7,3	2,6	0,0
Alvesta	6,8	0,8	0,0	5,6	0,0	3,4	1,5	0,6
Vetlanda	7,1	0,8	0,0	6,0	4,4	0,0	0,0	1,3
Low crop yield								
Reference	7,4	0,7	0,0	6,2	4,1	0,0	0,0	1,3
Osby	6,5	0,7	0,0	1,5	0,0	7,4	2,6	0,0
Alvesta	6,9	0,7	0,0	5,6	0,0	3,4	1,5	0,6
Vetlanda	7,2	0,7	0,0	5,1	4,1	0,7	0,0	1,5
High crop yield								
Reference	7,6	1,0	0,0	6,3	3,3	0,0	0,0	1,4
Osby	6,3	1,0	0,0	1,6	0,0	7,2	2,6	0,0
Alvesta	6,7	1,0	0,0	5,7	0,0	3,3	1,5	0,6
Vetlanda	7,6	1,0	0,0	6,3	3,3	0,0	0,0	1,4